

Fuzzy $\alpha - \psi^*$ - Irreducible Spaces



M. Rowthri, B. Amudhambigai

Abstract: In this paper, the concept of ψ^* operator on a family of fuzzy α -open sets in a fuzzy topological space is introduced. Also, the concepts of fuzzy $\alpha - \psi^*$ -irreducible spaces, fuzzy $\alpha - \psi^*$ -generic sets and fuzzy $\alpha - \psi^*$ -quasi-Sober spaces are initiated and some properties are discussed.

Keywords : operator on $F\alpha O(X, \tau)$, fuzzy $\alpha - \psi^*$ -generic sets, fuzzy $\alpha - \psi^*$ -irreducible spaces, fuzzy $\alpha - \psi^*$ -quasi-Sober spaces

2010 AMS Subject Classification: 54A40, 03E72..

I. INTRODUCTION

L.A. Zadeh[8] initiated fuzzy set in 1965. In 1968, Chang [2] characterized fuzzy topological space. Njastad [5] introduced α -open sets. In the same spirit Bin Shanna [1] defined fuzzy α -open sets and fuzzy α -closed sets. The idea of an irreducible or hyperconnected topological space has been studied by T. Thompson. In this paper, the concept of ψ^* operator on a family of fuzzy α -open sets in a fts is introduced. Also, the concepts of fuzzy $\alpha - \psi^*$ -irreducible spaces, fuzzy $\alpha - \psi^*$ -generic sets and fuzzy $\alpha - \psi^*$ -quasi-Sober spaces are initiated and some properties are discussed.

II. PRELIMINARIES

This section contains basic definitions and preliminary results needed for this paper.

Definition 2.1 [4] Let X be a topological space.

(i) X is irreducible, if $X \neq \Phi$, and whenever $X = Z_1 \cup Z_2$ with Z_i closed, $X = Z_1$ or $X = Z_2$.

(ii) $Z \subset X$ is an irreducible component of X if Z is a maximal irreducible subset of X .

Definition 2.2 [3] A subset $F \neq \Phi$ of a topological space is irreducible if, $F \subseteq A \cup B$ where A and B then $F \subseteq A$ or $F \subseteq B$.

Definition 2.3 [4] A topological space X is said to be quasi-sober if for every irreducible closed subset has a generic point.

Definition 2.4 [6] A fuzzy set μ_A is quasi-coincident with the fuzzy set μ_B iff $\exists x \in X$ such that $\mu_A(x) + \mu_B(x) > 1$.

Definition 2.5 [7] A fuzzy set λ in a fuzzy topological space (X, T) is called fuzzy dense if there exists no fuzzy closed set μ in (X, T) such that $\lambda < \mu < 1$. That is., $cl(\lambda) = 1$ in (X, T) .

Definition 2.6 [7] A fuzzy set λ in a fuzzy topological space (X, T) is called fuzzy nowhere dense if there exists no non-zero fuzzy open set μ in (X, T) such that $\mu < cl(\lambda)$. That is., $int(cl(\lambda)) = 0$ in (X, T) .

III. FUZZY $\alpha - \psi^*$ - IRREDUCIBLE SPACES

Throughout this paper, fuzzy topological space is shortly denoted by fts. Then $F\alpha O(X, \tau)$, $F\alpha C(X, \tau)$ and $\mathcal{FP}(X)$ denote set of all fuzzy α -open sets, fuzzy α -closed sets in (X, τ) and fuzzy points over X respectively.

Definition 3.1 Let (X, τ) be a fts. A fuzzy operator

$$\psi^*: F\alpha O(X, \tau) \rightarrow I^X$$

is defined as, if for each $\mu \in F\alpha O(X, \tau)$ with $\mu \neq 0_X$, $Fint(\mu) \leq \psi^*(\mu)$ and $\psi^*(0_X) = 0_X$.

Remark 3.1 It is easy to check that some examples of fuzzy operators on $F\alpha O(X, \tau)$ are the well known fuzzy operators viz. $Fint$, $Fint(Fcl)$, $Fcl(Fint)$, $Fint(Fcl(Fint))$ and $Fcl(Fint(Fcl))$.

Definition 3.2 Let (X, τ) be a fts and ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$. Then any $\mu \in F\alpha O(X, \tau)$ is called fuzzy $\alpha - \psi^*$ -open if $\mu \leq \psi^*(\mu)$. Then $1_X - \mu$ is called fuzzy $\alpha - \psi^*$ -closed set.

Notation 3.1 The family of all fuzzy $\alpha - \psi^*$ -open (resp. fuzzy $\alpha - \psi^*$ -closed) sets in (X, τ) is notated by $F\alpha - \psi^* O(X, \tau)$ (resp. $F\alpha - \psi^* C(X, \tau)$).

Definition 3.3 For any $\mu \in I^X$ in a fts (X, τ) and ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$, the fuzzy $\alpha - \psi^*$ -interior of μ (briefly, $F\alpha - \psi^* int(\mu)$) is defined by $F\alpha - \psi^* int(\mu) = \vee \{ \sigma : \sigma \leq \mu \text{ and } \sigma \in F\alpha - \psi^* O(X, \tau) \}$.

Definition 3.4 For any $\mu \in I^X$ in a fts (X, τ) and ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$, the fuzzy $\alpha - \psi^*$ -closure of μ (briefly, $F\alpha - \psi^* cl(\mu)$) is defined by $F\alpha - \psi^* cl(\mu) = \wedge \{ \sigma : \sigma \geq \mu \text{ and } \sigma \in F\alpha - \psi^* C(X, \tau) \}$.

Definition 3.5 Any fts (X, τ) is said to be a fuzzy $\alpha - \psi^*$ -irreducible space, where ψ^* is a fuzzy operator on $F\alpha O(X, \tau)$ if, for any

Manuscript received on April 02, 2020.

Revised Manuscript received on April 20, 2020.

Manuscript published on May 30, 2020.

* Correspondence Author

M. Rowthri*, Department of Mathematics, Sri Sarada College for Women(Autonomous), Salem, India. Email: rowth3.m@gmail.com

Dr. B. Amudhambigai, Department of Mathematics, Sri Sarada College for Women(Autonomous), Salem, India.. Email: rbamudha@yahoo.co.in

© The Authors. Published by Blue Eyes Intelligence Engineering and Sciences Publication (BEIESP). This is an open access article under the CC BY-NC-ND license (<http://creativecommons.org/licenses/by-nc-nd/4.0/>)

$\mu_1, \mu_2 \in F\alpha - \psi^*O(X, \tau)$ where $\mu_1 \neq 0_X, \mu_2 \neq 0_X$ and $\mu_1 q \mu_2$.

Definition 3.6 Any $\lambda \in I^X$ in a fts (X, τ) is said to be fuzzy $\alpha - \psi^*$ -irreducible, where ψ^* is a fuzzy operator on $F\alpha O(X, \tau)$ if, $\lambda \neq 0_X$ and $\lambda \leq (\mu_1 \vee \mu_2)$ where $\mu_1, \mu_2 \in F\alpha - \psi^*C(X, \tau)$, then either $\lambda \leq \mu_1$ or $\lambda \leq \mu_2$. Then the set of all fuzzy $\alpha - \psi^*$ -irreducible sets is noted by $F\alpha - \psi^*I(X, \tau)$

Definition 3.7 Any $\lambda \in I^X$ is called a fuzzy $\alpha - \psi^*$ -maximal irreducible set of fts (X, τ) , where ψ^* is a fuzzy operator on $F\alpha O(X, \tau)$, if there is no $\mu \in F\alpha - \psi^*I(X, \tau)$ such that $\mu > \lambda$. Then collection of all fuzzy $\alpha - \psi^*$ -maximal irreducible sets is denoted by $F\alpha - \psi^*MI(X, \tau)$

Definition 3.8 Let ψ^* be a fuzzy operator on $F\alpha O(X_1, \tau_1)$ and $F\alpha O(X_2, \tau_2)$ in a ftss (X_1, τ_1) and (X_2, τ_2) respectively. Any function $f : (X_1, \tau_1) \rightarrow (X_2, \tau_2)$ is said to be a fuzzy $\alpha - \psi^*$ -continuous function if for every $\mu \in F\alpha - \psi^*O(X_2, \tau_2)$, $f^{-1}(\mu) \in F\alpha - \psi^*O(X_1, \tau_1)$.

Proposition 3.1 Let ψ^* be a fuzzy operator on $F\alpha O(X_1, \tau_1)$ and $F\alpha O(X_2, \tau_2)$ in a ftss (X_1, τ_1) and (X_2, τ_2) respectively. Let $f : (X_1, \tau_1) \rightarrow (X_2, \tau_2)$ be a bijective and fuzzy $\alpha - \psi^*$ -continuous function. If $\lambda \in F\alpha - \psi^*I(X_1, \tau_1)$ then $f(\lambda) \in F\alpha - \psi^*I(X_2, \tau_2)$

Proof. Let $\mu_1, \mu_2 \in F\alpha - \psi^*C(X_2, \tau_2)$ such that $f(\lambda) \leq (\mu_1 \vee \mu_2)$. Then

$f^{-1}(f(\lambda)) \leq f^{-1}(\mu_1 \vee \mu_2)$, which implies that $\lambda \leq f^{-1}(\mu_1 \vee \mu_2)$. Then $f^{-1}(f(\lambda)) = \lambda$, since f is one-one. Thus $\lambda \leq f^{-1}(\mu_1) \vee f^{-1}(\mu_2)$. Since $\lambda \in F\alpha - \psi^*I(X_1, \tau_1)$, $\lambda \leq f^{-1}(\mu_1)$ or $\lambda \leq f^{-1}(\mu_2)$. Thus $f(\lambda) \leq f(f^{-1}(\mu_1))$ and hence $f(\lambda) \leq \mu_1$ as f is onto, $f(f^{-1}(\mu_1)) = \mu_1$.

or $f(\lambda) \leq f(f^{-1}(\mu_2))$ and so $f(\lambda) \leq \mu_2$. Therefore $f(\lambda) \in F\alpha - \psi^*I(X_2, \tau_2)$.

Remark 3.2 For any $\lambda \in I^X$ in a fts (X, τ) and ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$, $\lambda \leq F\alpha - \psi^*cl(\lambda)$.

Proof. Proof is obvious from the definition of fuzzy $\alpha - \psi^*$ -closure of a fuzzy set $\lambda \in I^X$.

Proposition 3.2 If $\lambda \in F\alpha - \psi^*I(X, \tau)$ in fts (X, τ) and ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$, then $F\alpha - \psi^*cl(\lambda) \in F\alpha - \psi^*I(X, \tau)$.

Proof. Assume that $\lambda \in I^X$ and $F\alpha - \psi^*cl(\lambda) \leq \mu_1 \vee \mu_2$ where $\mu_1, \mu_2 \in F\alpha - \psi^*C(X, \tau)$. Since $\lambda \leq F\alpha - \psi^*cl(\lambda)$ and $\lambda \in F\alpha - \psi^*I(X, \tau)$, $\lambda \leq \mu_1$ or $\lambda \leq \mu_2$. Then $F\alpha - \psi^*cl(\lambda) \leq \mu_1$ or $F\alpha - \psi^*cl(\lambda) \leq \mu_2$. Hence $F\alpha - \psi^*cl(\lambda) \in F\alpha - \psi^*I(X, \tau)$

Proposition 3.3. If $\lambda \in F\alpha - \psi^*MI(X, \tau)$, then $\lambda \in F\alpha - \psi^*C(X, \tau)$.

Proof. Let $\lambda \in F\alpha - \psi^*MI(X, \tau)$. Then, there is no $\mu \in F\alpha - \psi^*I(X, \tau)$ such that $\mu > \lambda$. By Proposition 3.2, $F\alpha - \psi^*cl(\lambda) \in F\alpha - \psi^*I(X, \tau)$. Since $\lambda \leq F\alpha - \psi^*cl(\lambda)$, the only possibility is $\lambda = F\alpha - \psi^*cl(\lambda)$. Hence $\lambda \in F\alpha - \psi^*C(X, \tau)$.

Proposition 3.4 Let $\lambda \in F\alpha - \psi^*MI(X, \tau)$ in fts (X, τ) , where ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$. If $\mu \in F\alpha - \psi^*I(X, \tau)$, then $\mu \leq \lambda$.

Proof. Let $\lambda \in F\alpha - \psi^*I(X, \tau)$. Let \mathcal{A} be the set of all fuzzy $\alpha - \psi^*$ -irreducible sets $\lambda_j \in I^X$ such that $\lambda < \lambda_j, j \in J$ where J is an indexed set. Let $\mathcal{A}' \subset \mathcal{A}$ be the set of fuzzy $\alpha - \psi^*$ -irreducible sets $\lambda_k, k = 1, 2, \dots, l$ such that $\lambda_1 < \lambda_2 < \dots < \lambda_l$.

Let $\lambda' = \bigvee_k \lambda_k, k = 1, 2, \dots, l$. It is enough to show that $\lambda' \in F\alpha - \psi^*I(X, \tau)$. Let $\lambda' \leq \mu_1 \vee \mu_2$, where $\mu_1, \mu_2 \in F\alpha - \psi^*C(X, \tau)$. Since each $\lambda_k \in F\alpha - \psi^*I(X, \tau), i = 1, 2, \dots, l$, we get $\lambda_i \leq \mu_1$ or $\lambda_i \leq \mu_2$. Suppose that for some $i_0 \in J, \lambda_{i_0} \in \mathcal{A}'$ and $\lambda_{i_0} \leq \mu_1$, then $\lambda_i \leq \mu_2$ for all $i \in J$. Thus $\lambda' \leq \mu_2$. Therefore $\lambda' \in F\alpha - \psi^*I(X, \tau)$ and $\lambda' \in F\alpha - \psi^*MI(X, \tau)$.

Proposition 3.5 If (X, τ) is fuzzy $\alpha - \psi^*$ -irreducible, then for any $\lambda \in F\alpha - \psi^*O(X, \tau)$, $F\alpha - \psi^*cl(\lambda) = 1_X$.

Proof. Since (X, τ) is fuzzy $\alpha - \psi^*$ -irreducible, for any two $\lambda, \mu \in F\alpha - \psi^*O(X, \tau)$ where $\lambda \neq 0_X$ and $\mu \neq 0_X$, $\lambda q \mu$. Let $\lambda_1 \in F\alpha - \psi^*O(X, \tau)$ such that $\lambda_1 \neq 0_X$. If $\lambda_1 = 1_X$, then $F\alpha - \psi^*cl(\lambda_1) = 1_X$. Assume that $\lambda_1 \neq 1_X$ and $x_{t_1} \in \mathcal{FP}(X)$ be such that $x_{t_1} \neq \lambda_1$. Let $\mu_1 \in F\alpha - \psi^*O(X, \tau)$ and $\mu_1 \neq 0_X$ such that $x_{t_1} \leq \mu_1$. By hypothesis, $\lambda_1 q \mu_1$. That is, there exist some $x_{t_i} \leq \lambda_1$ where $i \neq 1$ and $i \in J, J$ is an indexed set such that $x_{t_i} \leq \mu_1$ with $x_{t_i} \tilde{q} x_{t_1}$. Since μ_1 is an arbitrary fuzzy $\alpha - \psi^*$ -open set in (X, τ) , it follows that every fuzzy $\alpha - \psi^*$ -open μ_1 in (X, τ) is such that $x_{t_i} \leq \lambda_1$ and $i \in J$ such that $x_{t_i} \leq \mu_1$ with $\lambda_1 q \mu_1$. Therefore x_{t_i} is a fuzzy limit point of λ_1 . So every fuzzy point over X is a fuzzy limit point of λ_1 . Thus, every $x_{t_i} \in \mathcal{FP}(X)$ is such that $x_{t_i} \leq F\alpha - \psi^*cl(\lambda)$, $\lambda \in F\alpha - \psi^*O(X, \tau)$. Hence, fuzzy $\alpha - \psi^*$ -closure of every fuzzy $\alpha - \psi^*$ -open set is 1_X .

IV. FUZZY $\alpha - \psi^*$ -QUASISOBER SPACE

Definition 4.1 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Let $\lambda \in I^X$ be a fuzzy $\alpha - \psi^*$ -irreducible closed set. Any fuzzy set $\mu \in I^X$ with $\mu \leq \lambda$, is said to be a fuzzy $\alpha - \psi^*$ -generic set of λ if $F\alpha - \psi^*cl(\mu) = \lambda$.

Definition 4.2 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Then (X, τ) is said to be a fuzzy $\alpha - \psi^*$ -quasi-Sober space, if for every fuzzy $\alpha - \psi^*$ -irreducible closed set there exists a fuzzy $\alpha - \psi^*$ -generic set.

Remark 4.1 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Let $Y \subset X$ and (Y, τ_Y) be a fuzzy subspace of (X, τ) . Then ψ^* be a fuzzy operator on $F\alpha O(Y, \tau_Y)$.

Definition 4.3 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . If for $\lambda, \mu \in I^X$ with $\lambda q \mu$ there exists a $\delta \in F\alpha - \psi^* C(X, \tau)$ such that either $\mu \leq \delta$, $\lambda q \delta$ or $\lambda \leq \delta$, $\mu q \delta$, then (X, τ) is called fuzzy $\alpha - \psi^*$ -Kolmogorov.

Proposition 4.1 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Let $Y \subset X$ and (Y, τ_Y) be a fuzzy subspace of (X, τ) . If (X, τ) is fuzzy $\alpha - \psi^*$ -Kolmogorov, then (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -Kolmogorov.

Proof. Let $\lambda, \mu \in I^X$ with $\lambda q \mu$. Then there exists a $\delta \in F\alpha - \psi^* C(X, \tau)$ such that $\mu \leq \delta$, $\lambda q \delta$ or $\lambda \leq \delta$, $\mu q \delta$. Let $\lambda|_Y, \mu|_Y \in I^Y$ with $\lambda|_Y q \mu|_Y$. Since $\delta \in F\alpha - \psi^* C(X, \tau)$, $\delta|_Y \in F\alpha - \psi^* C(Y, \tau_Y)$. Also, since $\lambda|_Y \leq \lambda$, $\lambda \leq \delta$ and $\mu|_Y \leq \mu$, $\mu \leq \delta$, $\lambda|_Y \leq \delta|_Y$ with $\mu|_Y q \delta|_Y$ or $\mu|_Y \leq \delta|_Y$ with $\lambda|_Y q \delta|_Y$. Hence (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -Kolmogorov.

Notation 4.1 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ and $F\alpha O(Y, \sigma)$ where (X, τ) and (Y, σ) are any two fts. For any $\lambda \in I^X$, $\mu \in I^Y$, $F\alpha - \psi^* cl(\lambda)$ with respect to (X, τ) and (Y, σ) are denoted by $F\alpha - \psi^* cl(\lambda)$ and $F\alpha - \psi^* cl(\mu)$ respectively. Then the collection of all fuzzy $\alpha - \psi^*$ -irreducible closed in (X, τ) is denoted by $F\alpha - \psi^* IC(X, \tau)$

Proposition 4.2 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Let $Y \subset X$ and (Y, τ_Y) be a fuzzy $\alpha - \psi^*$ -closed subspace of (X, τ) . If (X, τ) is fuzzy $\alpha - \psi^*$ -quasi-Sober, then (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -quasi-Sober.

Proof. Let $\lambda \in F\alpha - \psi^* IC(Y, \tau_Y)$. Then $\lambda \in F\alpha - \psi^* IC(X, \tau)$. Since (X, τ) is fuzzy $\alpha - \psi^*$ -quasi-Sober, there exists a fuzzy $\alpha - \psi^*$ -generic set $\mu \in I^X$ such that $F\alpha - \psi^* cl(\mu) = \lambda$. Thus $F\alpha - \psi^* cl(\mu) \wedge 1_Y = \lambda \wedge 1_Y$. This implies that $F\alpha - \psi^* cl(\mu) \wedge 1_Y = \lambda$. Therefore $F\alpha - \psi^* cl(\mu) = \lambda$. Hence (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -quasi-Sober.

Proposition 4.3 Let ψ^* be a fuzzy operator on $F\alpha O(X_1, \tau_1)$ and $F\alpha O(X_2, \tau_2)$ where (X_1, τ_1) and (X_2, τ_2) are any two fts. Let $f: (X_1, \tau_1) \rightarrow (X_2, \tau_2)$ be an injective and fuzzy $\alpha - \psi^*$ -continuous function. If $\lambda \in F\alpha - \psi^* IC(X_1, \tau_1)$, then $F\alpha - \psi^* cl(f(\lambda)) \in F\alpha - \psi^* IC(X_2, \tau_2)$.

Proof. Let $\lambda \in F\alpha - \psi^* IC(X_1, \tau_1)$. Let $\mu_1, \mu_2 \in F\alpha - \psi^* C(X_2, \tau_2)$ such that $F\alpha - \psi^* cl(f(\lambda)) \leq \mu_1 \vee \mu_2$. Since $f(\lambda) \leq F\alpha - \psi^* cl(f(\lambda))$, $f(\lambda) \leq \mu_1 \vee \mu_2$. As f is injective, $\lambda \leq (f^{-1}(\mu_1)) \vee (f^{-1}(\mu_2))$. Then $\lambda \leq (\lambda \wedge f^{-1}(\mu_1)) \vee (\lambda \wedge f^{-1}(\mu_2))$. Since f is a fuzzy $\alpha - \psi^*$ -continuous function, $f^{-1}(\mu_1), f^{-1}(\mu_2) \in F\alpha - \psi^* C(X_1, \tau_1)$. This implies that $\lambda \wedge f^{-1}(\mu_1), \lambda \wedge f^{-1}(\mu_2) \in F\alpha - \psi^* C(X_1, \tau_1)$. Since $\lambda \in F\alpha - \psi^* IC(X_1, \tau_1)$, $\lambda \leq (\lambda \wedge f^{-1}(\mu_1))$ or $\lambda \leq (\lambda \wedge f^{-1}(\mu_2))$. Thus $\lambda \leq f^{-1}(\mu_1)$ or $\lambda \leq f^{-1}(\mu_2)$. Therefore, $f(\lambda) \leq \mu_1$ or $f(\lambda) \leq \mu_2$. This implies that $F\alpha - \psi^* cl(f(\lambda)) \leq \mu_1$ or $F\alpha - \psi^* cl(f(\lambda)) \leq \mu_2$. Hence $F\alpha - \psi^* cl(f(\lambda)) \in F\alpha - \psi^* IC(X_2, \tau_2)$.

Proposition 4.4 Let ψ^* be a fuzzy operator on $F\alpha O(X, \tau)$ in a fts (X, τ) . Let $Y \subset X$ and (Y, τ_Y) be a fuzzy $\alpha - \psi^*$ -open subspace of (X, τ) . If (X, τ) is fuzzy $\alpha - \psi^*$ -quasi-Sober, then (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -quasi-Sober.

Proof. Let $\mu \in F\alpha - \psi^* IC(Y, \tau_Y)$. Then $\mu \in F\alpha - \psi^* IC(X, \tau)$. Since (X, τ) is fuzzy $\alpha - \psi^*$ -quasi-Sober, there exists a fuzzy $\alpha - \psi^*$ -generic set $\lambda \in I^X$ such that $F\alpha - \psi^* cl(\lambda) = \mu$. Then $F\alpha - \psi^* cl_X(\lambda) \wedge \chi_Y = \mu \wedge \chi_Y$. Since $\mu \in F\alpha - \psi^* IC(Y, \tau_Y)$, $F\alpha - \psi^* cl(\lambda) = \mu$ and $\lambda \leq \mu$. Hence (Y, τ_Y) is fuzzy $\alpha - \psi^*$ -quasi-Sober.

V. CONCLUSION

In this paper, we explored ψ^* operator on a family of fuzzy α -open sets in a fuzzy topological spaces. We can extend ψ^* operator on fuzzy homotopy and fuzzy spectral spaces.

REFERENCES

1. A. S. Bin Shahna, On fuzzy strong semicontinuity and fuzzy precontinuity, Fuzzy Sets and Systems, vol.44, no.2, 1991, pp. 303-308.
2. C. L. Chang, "Fuzzy topological spaces", J. Math. Anal., Appl. 24, 1968, 182-190.
3. Z. Dondsheng, H. W. Kin, "On Topologies defined by Irreducible Sets", Journal of Logical and Algebraic Methods in Programming, 84, 2015, 185-195.
4. <https://stacks.math.columbia.edu/download/topology.pdf>
5. O. Njastad, "On some classes of nearly open sets", Pacific Journal of Mathematics, vol.15, 1965, 961-970.
6. P. M. Pu and Y. M Liu, "Fuzzy topology. I. Neighborhood structure of a fuzzy point and Moore-Smith convergence", J. Math. Anal Appl. 76, 1980, 571-599.
7. G. Thangaraj and G. Balasubramanian, On somewhat fuzzy continuous functions, The Journal of Fuzzy Mathematics, vol. 11, no. 2, 2003, pp. 725-736.
8. L. A. Zadeh, Fuzzy sets, Information and control, 8, 1965, 338-353.

AUTHORS PROFILE



M. Rowthri M.Sc.,M.Phil., is a research scholar in Mathematics in Sri Sarada College for Women(Autonomous), Salem, Tamilnadu, India. She has published three articles in national and international journals. She is doing research in fuzzy $\alpha - \psi^*$ — operator on fuzzy topological spaces.



Dr. B. Amudhambigai, M.Sc., MPhil, Ph.D is working as an Assistant Professor in Mathematics at Sri Sarada College for Women(Autonomous), Salem, Tamilnadu, India. She has published several articles in many reputed journals and guiding M.Phil and Ph.D students. Her research area includes fuzzy Cryptography and Mathematical Modelling.