

ARIMAX Model for Short-Term Electrical Load Forecasting



Shilpa G N, G S Sheshadri

Abstract: The scope for ARIMAX approach to forecast short term load has gained a lot of significant importance. In this paper, ARIMAX model which is an extension of ARIMA model with exogenous variables is used for STLF on a time series data of Karnataka State Demand pattern. The forecasting accuracy of ARIMA model is enhanced by taking into consideration hour of the day and day of the week as exogenous variables for ARIMAX model. Forecasting performance is thus improved by considering these significant load dependent factors. The forecasted results indicate that the proposed model is more accurate according to mean absolute percentage error (MAPE) obtained during the testing period of the model. As the historical load data are available on the databases of the utility, researches in the areas of time series modelling are ongoing for electrical load forecasting. In the proposed paper real time demand data available on Karnataka Power Transmission Corporation Ltd. (KPTCL) website is taken to develop and test the proposed load forecasting model. The power utility system operational costs and its security depend on the load forecasting for next few hours. Regional load forecasting helps in the accurate management performance of generation of power plant. Today's deregulated markets have great demand for prediction of electrical loads, required for generating companies. There has been tremendous growth in electric power demand and hence it is very much essential for the utility sectors to have their demand information in advance.

Index Terms: Artificial neural networks (ANN), autocorrelation, autoregressive integrated moving average with exogenous variables (ARIMAX), mean absolute percentage error, partial autocorrelation, short term load forecasting (STLF).

I. INTRODUCTION

Among the different categories of load forecasting, short-term load prediction has gained importance and has undoubtedly become an integral part in operational performance of any electric utility [1]. Some of the operational decisions namely economic scheduling of power station, fuel purchase schedule, energy transactions planning and power system security assessment [2]. In addition to power utilities other various firms like electricity marketers, traders and independent load system operators also need accurate load forecasts for their operations.

Hence, accurate and reliable electrical load forecasting can result in better financial rewards for all these entities. Accurate load predictions lead to great savings, as it improves economic load dispatch, unit commitment etc [3]. Many nonlinear factors like weather variables, daily, weekly and seasonal etc. practically affect STLF [4].

Several electrical utilities have adopted the conventional methods of forecasting the future loads. In conventional techniques, the models are mainly designed with respect to the relationship between the load and factors that influence the load power [5]. Recently, many similarity based approaches have been studied and developed for load forecasting. These approaches rely on the load behaviour information of the similar days that improves the forecasting accuracy. Such methodologies have the ability to deal with the nonlinear nature of the load along with its behavioural pattern in weekdays, weekends and special days/holidays [6-7]. Many researches have been carried out in the field of short term load forecasting [8]. Time Series Models and Artificial neural networks (ANN) are the main methodologies [9] used for load forecasting. Autoregressive integrated moving average (ARIMA) model is the best adopted procedure among various time series methods [10]. The modified form of ARIMA model is autoregressive integrated moving average (ARIMAX) model with exogenous variables. This method is implemented by applying the difference operation to get stationary time series. Then, the preliminary model order is identified and confirmed by analyzing the plots of the autocorrelation and partial autocorrelation [11]. The proposed model parameter estimation is done by applying maximum likelihood or weighted least-square methods [12]. As a result, electrical future load is forecasted based on intelligent projection of previous load and present load with greater reliability. The past load pattern of the power system and its constitution along with the distribution of region wise load is essential to get an overall good behaviour of load pattern. This paper presents time series ARIMAX modeling for STLF which takes into account hour of the day and day of the week along with the load as the inputs to the model. Practically, load depends on the hour of the day, day of the week; these significant factors should be taken into account for further improvement of the forecasting accuracy. Similarly other exogenous variables (special days, temperature etc.) that affect the load pattern can be included in the proposed ARIMAX modeling. This approach is analysed and simulated on a set of real time load data of Karnataka State Demand (2016).

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II. ARIMAXMODEL

The forecasting accuracy of ARIMA model is improved by addition of weekdays and weekends pattern that leads to ARIMAX model. Due to dynamic nature of the load, there exists a very strong correlation with the input variables selected. As a result, the forecasting performance of the ARIMAX model strongly depends on the input variables selected and the input variables are to be chosen in such a way that the forecasting error of the developed model is minimized.

Hourly load changes from one day to another day of the week affects the load pattern and hence becomes an important factor to be considered and included in the proposed ARIMAX model.

The ARIMAX model equation is given by,
 $A(q)y(t) = B(q)u(t) + C(q)e(t)$ ------(1)

where,

$A(q)$, $B(q)$ & $C(q)$ – Delay Polynomials

$u(t)$ - Exogenous Input Variables

$e(t)$ - Noise

$y(t)$ - Output Load

Autoregressive integrated moving average model with exogenous variables (ARIMAX) model development is mainly classified into three steps:

1. Determination of model order
2. Estimation of model parameters
3. Output load forecasting

The present paper attempts to simulate and execute all the three phases of ARIMAX approach in STLTF using real time load data of Karnataka Demand (2016). The proposed work is carried out using Mat lab software. Power grid demands accurate load forecasting that is essential for economic, stable and secure operation. It also helps in making proper necessary arrangements for planning the maintenance.

III. SIMULATION RESULTS

Statistical study of Karnataka State demand pattern is carried out for short term load forecasting. Analysis of simulation results & model development for accurate STLTF comprises of three major computational steps as explained below.

1. Determination of model order: Model is developed using January load data and tested on February load data. Fig.1 shows the plot of ACF for the month of January 2016. ACF plot indicates that the nature of the load is oscillatory and non-decaying. As a result, differencing of the load data is applied in order to make the set of considered load series stationary. Fig.2 shows the resulting auto correlation and partial autocorrelation plots for differenced set of time series load data. The initial order of the ARIMAX model is determined by studying and analyzing autocorrelation and partial autocorrelation plots for differenced time series load data.

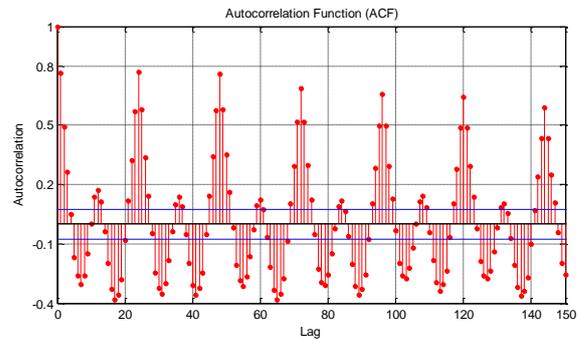


Fig.1. Plot of ACF for January load data.

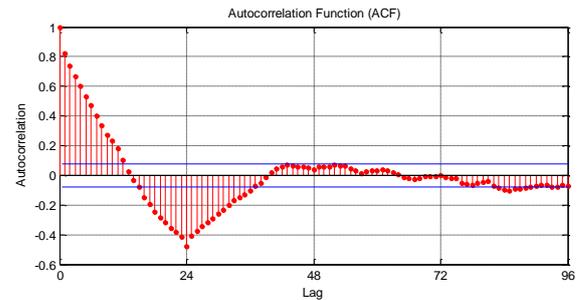


Fig.2. Plot of ACF for Differenced January load data

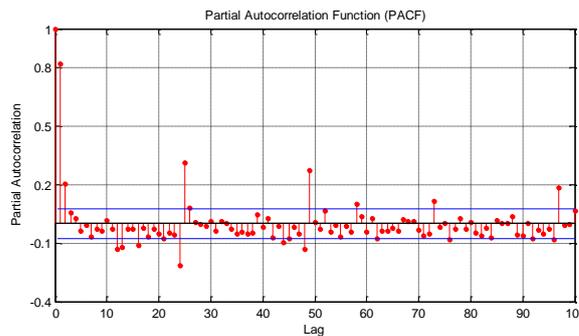


Fig.3. Plot of PACF for Differenced January load data

The ACF & PACF plots as shown in Fig.2 and Fig.3 suggest a model of order 2 i.e. autoregressive AR (2) and moving average MA (2). As a result, the developed ARIMAX (p,d, q) model takes the form ARIMAX (2, 1, 2)₂₄. After determining the orders of the model, the next step is to estimate the model parameters.

2. Estimation of model Parameters: In this phase, the proposed ARIMAX (2, 1, 2)₂₄ model estimates the values of coefficients of delay polynomials stated in equation (1) in order to minimize the energy of the noise term $e(t)$. Parameters are estimated by an efficient gradient based method known as the least square method. After all the parameters of ARIMAX (2, 1, 2)₂₄ model are estimated, the next step is to forecast the future values of the output load using this proposed model.

Figs.8-9 show load behaviour on weekdays and weekends. Monday through Saturday is taken as weekdays and Sunday is taken as weekend. The load pattern for weekdays and weekends of January/February month is analysed and it is observed that weekdays have similar pattern and weekends have similar pattern.

Hence ARIMAX (2, 1, 2)₂₄ model is developed that takes into consideration day code, hour code, weekdays and weekends as exogenous variables along with January (2016) load data of Karnataka State.

3. Output load forecasting: January load data is used to develop ARIMAX (2, 1, 2)₂₄ model and is applied to forecast the next month i.e. February hourly load. In order to check the ARIMAX model forecasting performance, it is essential to calculate the output load forecasting errors.

Fig.10 shows the proposed and developed model with Mean Absolute Percentage Error (MAPE) of 2.86%. The model outputs encouraging forecasting results with least forecasting errors. The forecasted results shown in Figs.4-7 indicate that the model is most suitable for short term load forecasting. Table I gives the weekly forecasted results (MAPE) for the month of February.

TABLE I ARIMAX Model Forecasted Results for February Month

WEEK	ARIMAX Model (Day code, hour code, weekends and weekdays) MAPE
1	3.48%
2	2.17%
3	2.38%
4	3.43%
Overall (February)	2.86%

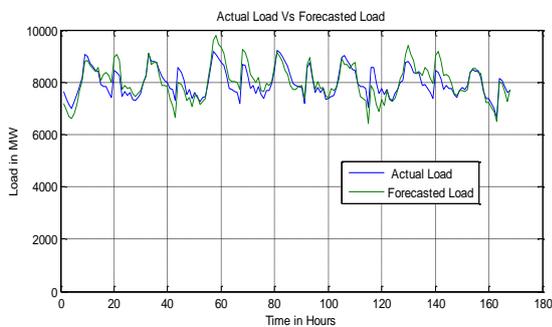


Fig.4 Forecasted result for 1st week (1/2 – 7/2 2016)

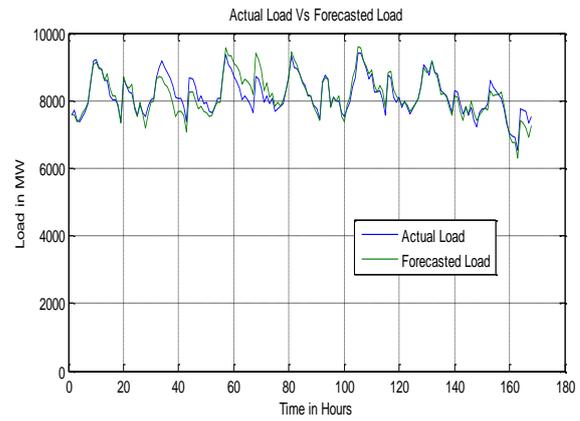


Fig.5 Forecasted result for 2nd week (8/2 – 14/2 2016)

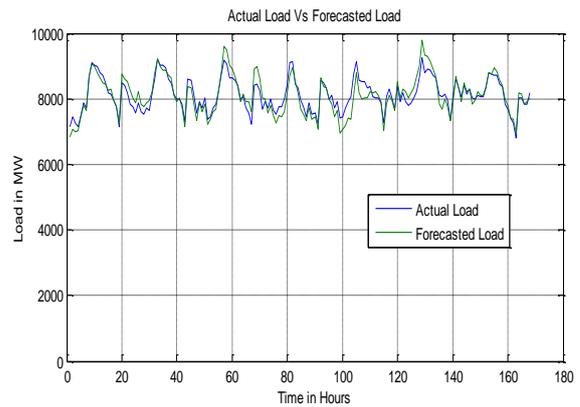


Fig.6 Forecasted result for 3rd week (15/2 – 21/2 2016)

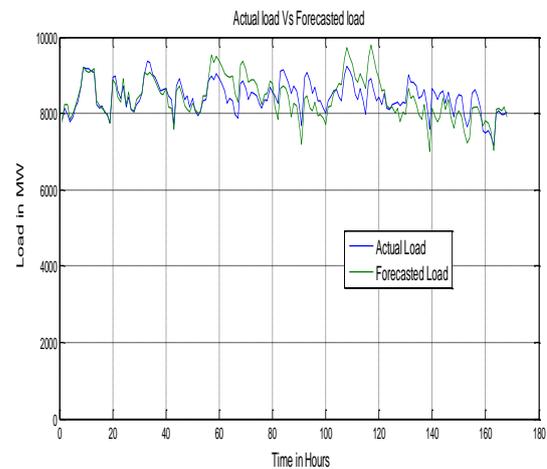


Fig.7 Forecasted result for 4th week (22/2 – 28/2 2016)

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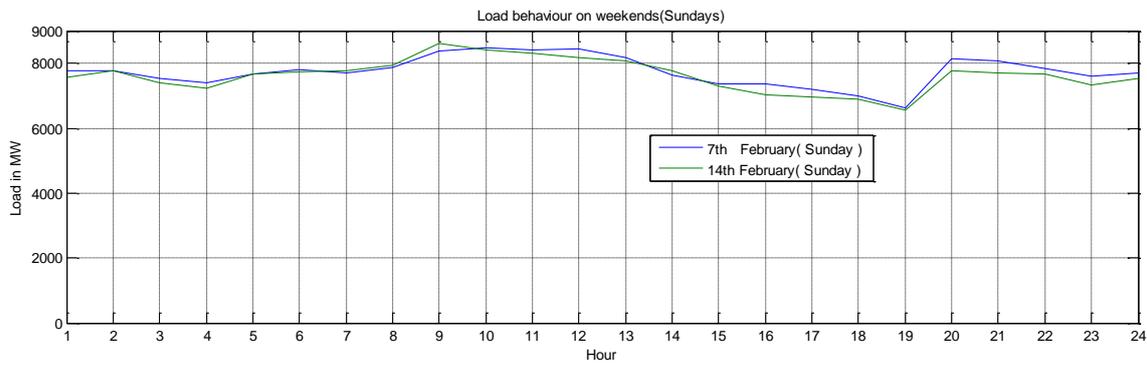


Fig.8 Load behaviour on weekends (Sundays) (07/2 &14/2 2016)

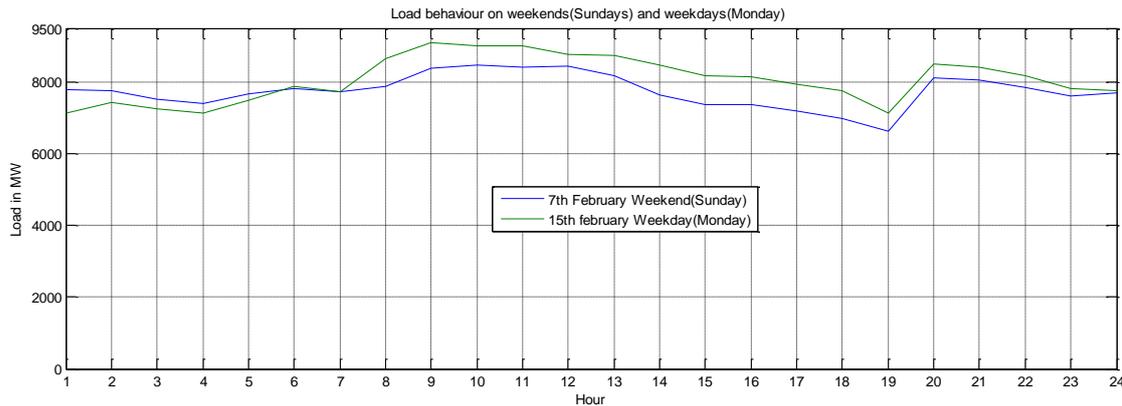


Fig.9 Load behaviour on weekends (Sundays) and weekdays (Monday) (07/2 &15/2 2016)

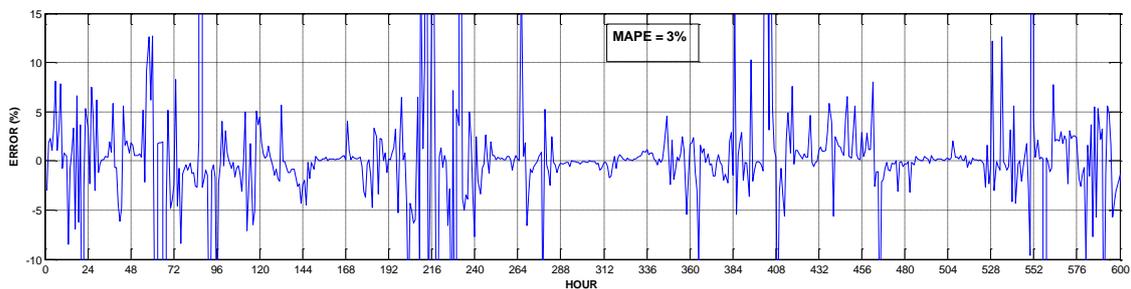


Fig.10 Mean Absolute Percentage Error (MAPE)

IV. CONCLUSION

The proposed ARIMAX model forecasts the electric load by considering the correlation established to the data of the selected similar days. Initially differencing is applied to January load data to make it stationary as it was observed to be oscillatory and non-decaying. Later the differenced data is used to build the model. The model orders were determined to be AR(2) and MA(2) by plotting PACF and ACF of differenced data respectively. The load pattern for weekdays and weekends of January/February month is analysed and it is observed that weekdays have similar pattern and weekends have similar pattern. Hence, the inputs chosen to build ARIMAX model are January month differenced hourly load data, time of the day, exogenous variables like weekdays and weekends. The model parameters are then estimated and February month load is forecasted. The forecasted load is compared with the actual load and forecasting errors are calculated. The results forecasted show a mean absolute percentage error (MAPE) of 2.86%. These research studies have reported that the load profile is dynamic in nature and hence the loads

are subjected to temporary and seasonal variations. Thus the electric load can be more accurately forecasted by considering these factors like temperature, humidity etc. that has major impact on the load.

REFERENCES

1. John Wiley and Sons Ltd. "Comparative models for electrical load forecasting", IEEE Transactions on Power Systems 1985.
2. Martin T Hagan & Suzanne M Bher "The Time Series Approach to Short Term Load Forecasting", IEEE Transactions on Power Systems, Vol. PWRS-2, No.3, pp.785-790, August 1987.
3. Nima Amjadi "Short-Term Bus Load Forecasting of Power Systems by a New Hybrid Method", IEEE Transactions on Power Systems, Vol.22, No.1, pp.392-401, February 2007.
4. Ching-Lai Hor, Simon J. Watson & Shanti Majithia "Analysing The Impact of Weather Variables On Monthly Electricity Demand", IEEE Transactions on Power Systems, Vol.20, No.4, pp.2078-2085, November 2005.
5. Ibrahim Moghram & Saifur Rahman "Analysis And Evaluation Of Five Short-Term Load Forecasting Techniques", IEEE Transactions on Power Systems, Vol.4, No.4, pp.1484-1490, October 1989.

7. M Nakamura, "Short Term Load Forecasting Using Weekday load Models and Bias Models", Proc. PICA Conference, pp. 37-42, 1984.
8. Hong-Tzer Yang, Chao-Ming & Ching-Lein Huang "Identification of ARMAX Model For Short Term Load Forecasting: An Evolutionary Programming Approach", IEEE Transactions on Power Systems, Vol.11, No.1, pp.403-408, February 1996.
9. IEEE Committee Report, "Load Forecasting Bibliography Phase I", IEEE Trans. on Power Appr. and Sys., Vol. PAS-99, pp. 53-58, 1980.
10. Shilpa.G.N, Dr.V.Venkatesh, Nataraja.C "Study & Development of Short Term Load Forecasting Models Using Stochastic Time Series Analysis" International Journal of Engineering Research and Development, Vol 9, Issue 11, PP. 31-36, February 2014.
11. Shilpa.G.N, Dr.G.S.Sheshadri, "Short Term Load Forecasting Using ARIMA Model For Karnataka State Electrical Load", International Journal of Engineering Research and Development", Vol 13, Issue 7, PP. 75-79, July 2017.
12. Shilpa.G.N "Short Term Load Forecasting Using Time Series Analysis: A Case Study for Karnataka, India", International Journal Of Engineering Science And Innovative Technology, Vol 1, Issue 2,PP. 45-53, November 2012 .
13. "Short Term Power System Load Forecasting Using the Iteratively Reweighed Least Squares Algorithm", Electric power system research, 19 (1990) pp. 11-12.
14. T Haida and S Muto, "Regression Based Peak Load Forecasting using a Transformation Technique", IEEE Trans. Power syst., Vol. 9, pp. 1788-1794, Nov. 1994.
15. S Rahman and O Hazim, "A generalized Knowledge-Based Short Term Load Forecasting Technique", IEEE Trans. Power syst., Vol. 8, pp. 508-514, May 1993.
16. Gross G and Galiana F D, "Short-Term Load Forecasting", Proc. IEEE, Vol. 75, No 12, pp. 1558-1573, 1987.
17. Alex D and Timothy C, "A Regression-Based Approach to Short-Term System Load Forecasting", IEEE Trans. Power syst., Vol. 5, No 4, pp. 1535-1547, 1990.

AUTHORS PROFILE



Shilpa G N received her B.E. Degree in Electrical and Electronics Engineering in 2003 from Visvesvaraya Technological University and M.E. in Power and Energy Systems from University Visvesvaraya College of Engineering, Bangalore University, Karnataka, India. From 2007 through 2009, she had been working as Assistant Professor in Bapuji Institute of Engineering and Technology, Davangere.

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