

# Mixed Convective Flow of a Visco Elastic Fluid Between Two Porous Parellel Plates



D Satish Kumar, C.H.V Ramana Murthy, S. Anusha, Oluwole. D. Makinde

*Abstract— A diagnostic answer for the problem of sincerely grew loose convective circulation between two vertical parallel plates has been inspected in this paper. The trademark highlights of various parameters were talked about in element. it's miles considered that to be the Grashoff huge variety declines, the profiles are more and more illustrative in nature. Likewise, due to the fact the Grashoff range reductions the charge of the liquid medium increments. it is found that, the pinnacle pace is type of organized at a median separation most of the circulate geometry. similarly, as the Grashoff amount reductions, the imply essential thrust gives off an influence of being step by step main as impact of which the liquid movements quicker within the middle locale. Likewise, it is visible that, the speed increments because the Prandtl quantity discounts. in addition, it is considered that to be the Prandtl variety expands the mass transition diminishes. The mass transition is absolutely constrained thru the parameters, for instance, Reynolds range and Prandtl amount. The flow into supporter in each the instances does no longer differs lots. All above said outcomes and delineations accommodate with the outcomes built up by manner of M. Sajid, I. Pop, T. Hayat*

## I. INTRODUCTION

The development of heat skip of viscoelastic beverages has significantly elevated applications within the regions of Geothermal power extraction, catching of sun powered energy, Oil extraction from the profound earth outside and so on. The situations of motion of non-Newtonian liquids are profoundly non-direct. The enlargement of the hypothesis of Newtonian liquid mechanics to the non-Newtonian beverages isn't so easy. The shear subordinate consistency of the liquid medium could make the overseeing situations of the movement just as the speculation profoundly entangled. due to the semi direct fame of the overseeing circumstance of movement, getting the cautious arrangement isn't that fundamental real to shape inside the direction of recent many years. For non-Newtonian liquids, locating genuine arrangements isn't always easy. in this regard, the effects of

liquid shear-diminishing behavior on its pores and skin contact coefficient were settled in the course of the years Acrivos et al. [1]; Schowalter [2]; Pakdemirli [3]; Rajagopal et al. [4]; Labropulu and Chinichian [5] and so forth.

Warmth drift in unfastened and blended convection in vertical channels has some mechanical and common place packages. In this way, it's been the scenario of changed pastimes. For the maximum component, numerical solution for several circulate setup of the applications happens in the plan of cooling frameworks for virtual devices and in acquiring sun oriented power. some creators had factor by way of way of element assessment of the temperature and pace profiles for the vertical and parallel actually created times. among such experts are Aung and Worku [6], Cheng et al. [7], Barletta [8,9], Barletta and Zanchini [10], Chamkha [11], Barletta et al. [12], El-Din [13]

The warmth alternate innovation that is generally applied in cooling of digital gadgets consists of convective streams in vertical channels, in such conditions those streams infer states of uniform warm temperature of the channel and uniform warm temperature movement heat restrict conditions. The above examination of free and mixed convection movement in vertical channels depend on the hypothesis that the drinks are Newtonian. this means, the pressure is straightforwardly much like strain price. In view of the vital and mechanical significance exam with reference to loose, restricted and mixed convective progression of non-Newtonian drinks in the channel and cylinders and annulus are giant. The applications are more and more thorough in some territories of mechanical and current fields.

A medical answer for the problem of completely grew free convective progression of a small scale polar liquid among vertical parallel opinions has been analyzed via Chamka et al [14]. alongside the ones traces, the actually created circulation and warmth drift of an electrically principal small scale polar liquid among two vertical permeable parallel plates inside the sight of temperature ward warm temperature resources and within the sight of executed attractive discipline became analyzed via using Bhargava et al [15]. For this case the overseeing ODE state of affairs has been defined numerically through Quasi linearization technique. From that factor, Ariel [16] displayed an investigative answer for 2 troubles of laminar confined convection of a Rivlin Ericksen liquid through parallel permeable dividers. As of late, in an investigation displayed by way of way of Hayat and Abbas [17] inspected 2nd restrict layer flow of an higher convective Maxwell liquid in a channel with the aid of thinking about the compound response within the center.

Manuscript published on 30 September 2019

\* Correspondence Author

**D. Satish Kumar\***, Department of Mathematics, Koneru Lakshmaiah Education Foundation, Vaddeswaram, Guntur, Andhra Pradesh, India.  
(Email: satish9441321888@gmail.com)

**C.H.V Ramana Murthy**, Department of Mathematics, Koneru Lakshmaiah Education Foundation, Vaddeswaram, Guntur, Andhra Pradesh, India.

**S. Anusha**, Department of Mathematics, Koneru Lakshmaiah Education Foundation, Vaddeswaram, Guntur, Andhra Pradesh, India.

**Oluwole. D. Makinde**, Applied Mathematics Department, Stellenbosch University, South Africa.

© The Authors. Published by Blue Eyes Intelligence Engineering and Sciences Publication (BEIESP). This is an [open access](https://creativecommons.org/licenses/by-nc-nd/4.0/) article under the CC-BY-NC-ND license <http://creativecommons.org/licenses/by-nc-nd/4.0/>

The dividers of the channels are seemed as permeable and likeness modifications are implemented to the administering nonlinear midway differential condition. The Nonlinear midway differential

situation are modified into nonlinear regular differential condition. answer for any such condition is gotten by using the usage of making use of HAM approach as proposed with the resource of Liao [18]. Be that as it could, to the amazing of the creators analyzing the iconic blended convective progression of viscoelastic liquid in a parallel vertical channel has now not been targeted in itemized. Such an investigation is wanted for know-how the pass profiles or the best and secure trademark highlights. Underneath the circulate presumptions, the important administering situation of movement may be dwindled ODE which may be tackled diagnostically. The impacts of suitable parameters, as an instance, viscoelasticity of the medium, suction of the infusion parameter, the Grashoff huge variety, Reynolds range has been tested in nitty gritty. The impacts of such parameters and tempo and pores and skin grinding has among represented graphically.

1. Primary Equations growth textual content size

take into account a viscoelastic liquid which always streams among porous interminable vertical and parallel plane dividers. The separation the various dividers, as an instance the channel width, is L. An arrange framework is picked to such an quantity that the x-hub is parallel to the gravitational dashing up vector g, but with the other manner. The y-hub is symmetrical to the channel dividers, and the inception of the tomahawks is with the stop goal that the locations of the channel dividers are y=zero and y=L, individually. A comic strip of the framework and of the set up tomahawks is accounted for in Fig. 1. The divider at y=0 is at the given uniform temperature T2, while the divider at y= L is exposed to a uniform temperature T1 in which T2>T1. The liquid pace vector v=(u, v) is notion to be parallel to the x-pivot, so really the x-section u of the rate vector would not evaporate but the transpiration move-move speed remains steady, in which  $\tau$  is the rate of suction and is the rate of infusion. The Boussinesq guess is implemented. all the liquid houses aside from thickness in the lightness term are taken into consideration as ordinary. The flow into being really built up, the accompanying relations observe proper here:

$$v = v_0 = const. \quad \frac{\partial u}{\partial x} = 0, \quad \frac{\partial u}{\partial y} = \frac{du}{dy}$$

$$\frac{\partial p}{\partial y} = 0, \quad \frac{\partial p}{\partial x} = \frac{dp}{dx} = const. \quad (1)$$

$$\frac{\partial T}{\partial x} = 0, \quad \frac{\partial T}{\partial y} = \frac{dT}{dy}$$

Thus, the basic governing equations are transformed to:

$$\rho v_0 \frac{du}{dy} = -\frac{dp}{dx} + \mu \frac{d^2u}{dy^2} + \alpha_1 v_0 \frac{d^3u}{dy^3} + \rho g \beta (T - T_0) + Hu \quad (2)$$

$$v_0 \frac{dT}{dy} = \alpha \frac{d^2u}{dy^2} \quad (3)$$

while the boundary conditions are:

$$u(0) = u(L) = 0$$

$$T(0) = T_1, \quad T(L) = T_2 \quad (4)$$

Were the pressure gradient  $\frac{dp}{dx}$  in equation (2) is unknown and must be evaluated via the overall mass conservation equation

$$\int_0^L u dy = Q \quad (5)$$

We introduce new following dimensionless variables:

$$Y = \frac{y}{L}, \quad U = \frac{u}{U_0}, \quad \theta = \frac{T - T_0}{T_2 - T_0} \quad (6)$$

The equations (2) and (3) in the non-dimensional form are:

$$KR \frac{d^3U}{dY^3} + \frac{1}{\rho} \frac{d^2U}{dY^2} - R \frac{dU}{dY} + A + \frac{Gr}{Re} \theta = 0 \quad (7)$$

$$\frac{d^2\theta}{dY^2} - RPr \frac{d\theta}{dY} = 0 \quad (8)$$

while the boundary condition (4) now become

$$U(0) = U(1) = 0, \quad \theta(0) = r_\tau, \quad \theta(1) = 1 \quad (9)$$

Along with overall mass conversation equation

$$\int_0^1 U dY = 1 \quad (10)$$

Considering  $Q = U_0 L$  the dimensionless parameters, viscoelastic parameter(K) The Suction or injection parameter (R),Grashoff number (Gr), The Reynolds number( Re),

the wall Temperature parameter ( $r_\tau$ ), Prandtl Number (Pr), Constant Pressure gradient (A) are defined as:

$$K = \frac{\alpha_1}{\rho L^2} \quad R = \frac{v_0 L}{V} \quad Gr = \frac{g \beta (T_2 - T_0) L^3}{\mu v_0}$$

$$Re = \frac{v_0 L}{\nu} \quad Pr = \frac{\nu}{\alpha} \quad r_\tau = \frac{T_1 - T_0}{T_2 - T_0} \quad A = -\frac{L^2}{u_0 \nu \rho} \frac{dp}{dy} \quad (11)$$

It is mentioned that when K=0 (Newtonian fluid) & R=0 (Non-porous walls)

Solution for a Newtonian Fluid

When k=0 the solution for the boundary value problems (7) and (8) subject to conditions (9) is straight forward and is given by

$$U = \frac{A}{C} + \frac{Gr}{Re C} \frac{1 - r_\tau e^{RP_r}}{1 - e^{RP_r}} + \frac{r_\tau - 1}{1 - e^{RP_r}} \frac{e^{RP_r Y}}{R^2 P_r [KR^2 P_r^2 + P_r - 1]} + c$$

$$+ C_1 e^{\frac{R + \sqrt{R^2 - 4c}}{2} Y} + C_2 e^{\frac{R - \sqrt{R^2 - 4c}}{2} Y} \quad (12)$$



Clearly  $R^2 - 4c > 0$

$$\theta = \frac{1 - r_T e^{RP_r}}{1 - e^{RP_r}} + \frac{r_T - 1}{1 - e^{RP_r}} e^{RP_r Y} \quad (13)$$

Where  $c_1, c_2$  are arbitrary constants evaluated using (9).

## II. RESULTS AND DISCUSSION.

Fig 1 Illustrates the velocity profiles for constant values of viscoelastic parameter(K) The Suction or injection parameter (  $R$  ), Grashoff number (  $G_r$  ), The Reynolds number (  $Re$  ), the wall Temperature parameter (  $r_T$  ), Prandtl Number (  $Pr$  ), Constant Pressure gradient (  $A$  ). The profiles are indicating for different values Grashoff number (  $Gr$  ). It is seen that, as the  $Gr$  decreases the profiles of more parabolic in nature. Also, as the  $Gr$  decreases the velocity of the fluid medium increases and the peak velocity is almost situated at a mean distance in the flow geometry. Further, as the  $Gr$  decreases, the mean driving force appears to be more prominent as result of which the fluid velocity is more prominent as result of which the fluid moves at a faster.

Fig.2 depicts the velocity profiles for different values of Prandtl number and for constant values of  $r_T, K, A, R, Gr, Re$ , It is noticed that, the velocity

profiles are more parabolic as the Prandtl number decreases. Also, it is observed the velocity increases as the Prandtl number decreases. In this case the driving force necessary for the fluid to set into the motion is more dominating than the Prandtl values.

Fig.3 illustrates the heat flux for different values of Reynolds number as it is observed as  $y$  increases the mass flux also increases for constant values of  $r_T$  and  $Pr$  as  $R$  increases the mass flux decreases. This is due to the fact that the Reynolds number significantly influences the flow pattern. Hence the conclusion.

Fig.4 exhibits the behavior of mass flux with respect to the Prandtl number for constant values of the wall temperature parameter and Suction or Injection parameter. It is noticed that, as the Prandtl number increases the mass flux decreases. Also, as  $y$  increases the mass flux is observed to increasing. It can be concluded that the Prandtl number significantly influences the flow pattern.

In view of above conclusions from fig.3 and fig.4, the mass flux is totally controlled by the parameters such as Reynolds number and Prandtl number. The flow pattern on in both the cases does not varies much.

All above said results and illustrations reconcile with the results established by M. Sajid, I. Pop, T. Hayat [19]. However, the procedure illustrated differ significantly while the conclusions remains same.

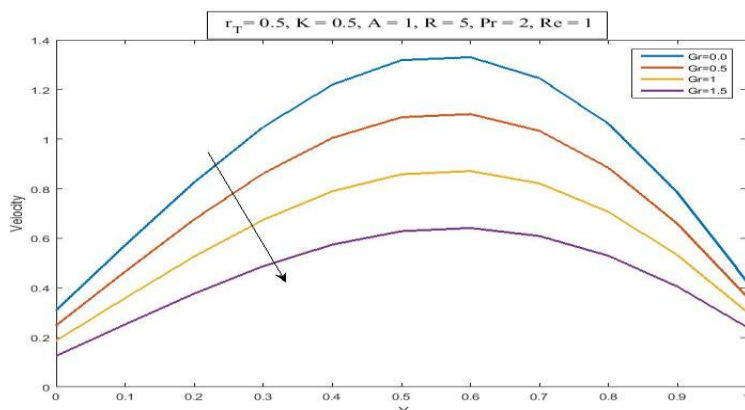


Fig-1 Influence of Grashof number (Gr) on the velocity.

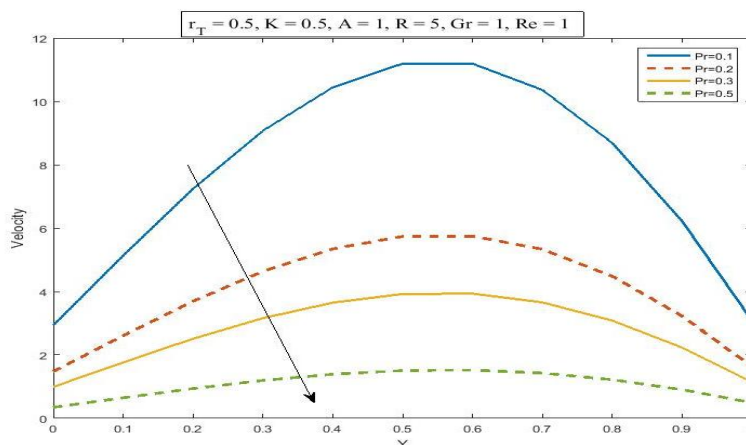


Fig-2 Influence of Prandtl number (Pr) on the velocity.

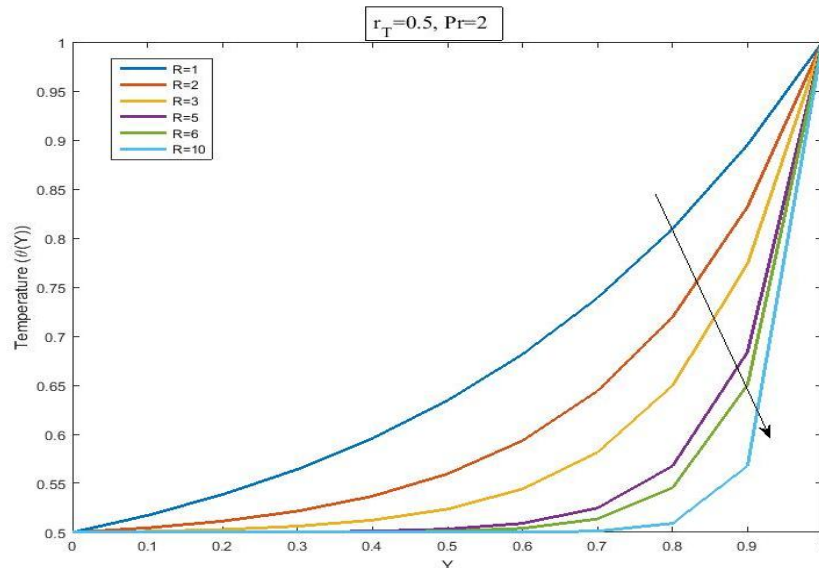


Fig-3. Influence of Prandtl number (Pr) on the temperature.

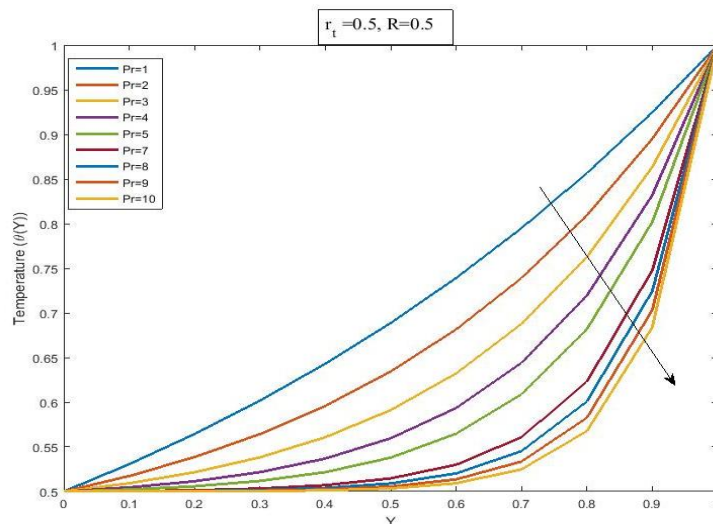


Fig-4 Influence of Prandtl number(Pr) on the temperature.

REFERENCES

- 1 Acrivos, M.J. Shah, E.E. Peterson, Momentum and warmth transfer in laminar boundary-layer waft of non-Newtonian fluids beyond outside surfaces, *AICHE J.* 6 (1960) 312-317.
- 2 W.R. Schowalter, The application of boundary-layer precept to power-law pseudoplastic fluids: Similarity answers, *AICHE J.* 6 (1960) 24-28.
- 3 M. Pakdemirli, Boundary layer go with the flow of electricity-regulation fluids past arbitrary profiles, *IMA J. Appl. Math.* 50 (1993) 133-148.
- 4 k.R. Rajagopal, A.S. Gupta, A.S. Wineman, On a boundary layer precept for non-Newtonian fluids, *Appl. Sci. Eng. Lett.* 18 (1995) 875-883.
- 5 W. Aung, G. Worku, precept of virtually developed, blended convection including go together with the drift reversal, *J. Warmth switch* 108 (1986) 485-488.
- 6 C.-H. Cheng, H.-S. Kou, W.-H. Huang, float reversal and warmth transfer of without a doubt developed combined convection in vertical channels, *J. Thermophysics* 3(1990) 375-383.
- 7 k. Boulama, N. Galanis, Analytical solution for in truth superior combined convection among parallel vertical plates with warmth and mass switch, *J. HeatTransfer* 126 (2004) 381-388.
- 8 A. Barletta, Laminar blended convection with viscous dissipation in a vertical channel, *Int. J. Warmness Mass transfer* 41 (1998) 3501-3513.
- 9 A. Barletta, evaluation of combined forced and free float in a vertical channel with viscous dissipation and isothermal\_isoflux boundary situations, *ASME J. Warmth switch* 121 (1999) 349-356.
- 10 A. Barletta, E. Zanchini, On the selection of the reference temperature for absolutely advanced combined convection in a vertical channel, *Int. J. Heat Mass Transfer*42 (1999) 3169-3181.
- 11 A.J. Chamkha, waft of immiscible fluids in porous and nonporous channels, *J. Fluids Eng.* 122 (2000) 117-124.
- 12 A. Barletta, E. Magyari, B. Keller, twin combined convection flows in a vertical channel, *Int. J. Warmness Mass transfer* forty eight (2005) 4835-4845.
- 13 [13] M.M. Salah El-Din, impact of thermal and mass buoyancy forces on the development of laminar blended convection among vertical parallel plates with uniform wall heat and mass fluxes, *Int. J. Thermal Sci.* Forty

- (2003) 447-453. [14] A.J. Chamkha, T. Grosan, I. Pop, Fully developed free convection of a micropolar fluid in a vertical channel, *Int. Commun. Heat Mass Transfer* 29 (2002) 1021-1196.
- 14 R. Bhargava, L. Kumar, H.S. Takhar, Numerical solution of free convection MHD micropolar fluid glide between parallel porous vertical plates, *Internat. J. Engrg. Sci. Forty one* (2003) 123-136.
- 15 P.D. Ariel, On genuine answers of float issues of a 2nd grade fluid via parallel porous partitions, *Internat. J. Engrg. Sci.* 40 (2002) 913-941.
- 16 T. Hayat, Z. Abbas, Channel flow of a Maxwell fluid with chemical reaction, *J. Appl. Math. Phys. (ZAMP)* 59 (2008) 124\_144.
- 17 S.J. Liao, beyond Perturbation: creation to Homotopy evaluation method, Chapman & hall/CRC Press, Boca Raton, 2003.
- 18 M. Sajid, I. Pop, T. Hayat, completely evolved blended convection float of a viscoelastic fluid between permeable parallel vertical plates, computer systems and arithmetic with packages 59 (2010) 493-498