Radon Transform Based Modified Nonlinear Access for Segmentation of Mammogram Application

Saikumar Tara, R.Nirmala Devi

Abstract--- In this paper a novel and application oriented mammogram segmentation using Nonlinear level set method and Radon Transform proposed. Handling medical images as a part of segmentation issues plays a critical phase. The proposed approach of nonlinear method of segmentation for which specific images of mammogram are consideredusing probability weighted force stopping function and Bayesian rules to extract the weak boundaries. This proposed method leads to get true extract boundaries and also minimizes the boundary leakagesusing this approach.The experiment demonstration with suitable images are performed on LSF.

Keywords— LSF, Radon transform, Segmentation, Mammogram.

I. INTRODUCTION

Image segmentation is a fundamentalstep of image exploration, and basisunderstanding ofthe image attitudes. Image segmentation refers to the modern technology and essential component in the modern era of active research which decomposes images into aregions and extracts the area of interested or region targets. It is also a part of computer vision as a part of image acquires and understanding. Image segmentation overlaps between image processing and image analysis in domain of image processing. The amount of quality in the segmentation results will always directly affect the human visional performances. With the horizon development of the image domain such as biology, computer science, pattern recognition, image segmentation technology and many more [1].Closed curve of snake model varies in accordance with partial Difference Equation as a spectrum of Contour. A family of PDE is a kind of Jacobi series of equation from Euler Lagrange equation as a part of predefined novel minimization of energy. The main function of a contour is to handle the closed curve by changing its characteristics graphically. Level Set Method is divided in to two phrases such as edge based segmentation and region based segmentation for an active contour in an image [2-3].

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Role of boundary leakages problems are a key issues in the area of image segmentation as apart of image processing which indeed needed to control the boundary leakages as a sensitive issues with a nonlinear approach and Level Set Method by combining edge indicator function and based on region force stopping approach for an energy functional [4]. The nonlinear approach of segmentation has few advantages such as direction force function is designed based on the curve evolution and its initial position which indeed remove the occurrences of leakages for weak boundaries. The Bayesian rule with weighted stopping force is designed to identify the false boundaries edges for a specified applications of an images.

II. EXISTING LEVEL SET METHOD

A Level set function shall be defined as its value is set to be zero level set if an only if its signed distance function is not zero with which the segmentation will not be true. With the help of partial differential equation for calculation of curve evolution to rebuild level set function [10]. The computational cost function can be obtained after the executation of few iteration steps which will be reinitialized.

Li et al, proposed a term call energy functional [4]

$$E_g = E_1 + E_2 + E_3 ------(1)$$

$$E_1 = \mu \int_{\xi} \frac{1}{2}(|\nabla \phi| - 1)^2 ----(2)$$

$$E_2 = \lambda \int_{\xi} g\delta(\phi)|\nabla \phi| dxdy ----(3)$$

$$E_3 = \vartheta \int_{\xi} gH(-\phi)dxdy -----(4)$$

where ξ denotes the image domain and ϕ is LS (level set).The Three items in the above equation are a signed function which is used [5]. The parameter such as μ , λ ϑ are the weight controls of convergence speed. H(.) is a Heaviside Function [10].

$$g = \frac{1}{1 + |\nabla G_\sigma .I|^2} ----(5)$$

Where G_σ is a Gaussian Function with a standard deviation, σ ; I is the mammogram image.

As upon solving PDE the two external popular energy functions which has a drawback of shrink and also stopping function g which leads to against of noise. Chan andVese [5] proposed a region based level set method by using piecewise constant function to be segmented.

The external energy functional are

$$E_g(\phi) = \nu_1 + \nu_2 + \nu_3 + \nu_4 ----(6)$$

$$\nu_1 = \mu \int_{\xi} \delta(\phi) |\nabla \phi| dxdy -----(7)$$

$$\nu_2 = \vartheta \int_{\Omega} H(\phi) dxdy ----(8)$$

$$\nu_3 = \lambda_1 \int_{inside(\varpi)} |I - c_1|^2 dxdy -----(9)$$

$$\nu_4 = \lambda_2 \int_{outside(\varpi)} |I - c_2|^2 dxdy -----(10)$$

where c_1 and c_2 are grayscale mean values of pels inner and outer curve respectively.

To handle over a complex situation problems designed by Chen and Tseng [6] on level set method and also global energy functional is

$$F(\varpi, \phi) = \mu \int_{\xi} \delta(\phi) |\nabla \phi| dxdy + \sum_{i=1}^{2} \int_{\omega_i} p(\omega_i) p\left(I / \omega_i \right) dxdy -----(11)$$

where ω_1 and ω_2 denote the curves of inner and outer.

Considering the conditional probability in above equation is purely Gaussian distribution and applying the logarithm operation so we have

$$\sum_{i=1}^{2} \int_{\omega_i} \log p(\omega_i) - \frac{1}{2} \left(\left(\log(2\pi\sigma_i^2) \right) + \frac{(I - \mu_i)^2}{\sigma_i^2} \right) dxdy -----(12)$$

The Bayesian terms appearing in above equations (6) and (11) which viewed as standardized statistical equation of (6)

III. IMPROVED NON LINEAR LEVEL SET METHODS

The pre-requisition, the adaptive direction function which is defined over an image domain of $\xi = \xi_1 + \xi_2$, where ξ_1 and ξ_2 represent the object and background [6].

$$f(x, y) = p\left(\frac{\xi_1}{I^*(x, y)} \right) - T_p -----(13)$$

T_p is consider as threshold.

The energy functional defined on LSF ϕ is the level set framework for segmentation of an image with different gradients. A non linear adaptive function is with the help of stopping function of the weighted probability to obtain the energy function [4],[7],[9], i.e.,

$$E(\phi) = \psi_1 + \psi_2 + \psi_3 ----(14)$$

$$\psi_1 = \mu \int_{\Omega} \frac{1}{2} (|\nabla \phi| - 1)^2 dxdy -----(15)$$

$$\psi_2 = \lambda_1 \int_{\Omega} \frac{\delta(\phi) |\nabla \phi|}{\Psi} dxdy -----(16)$$

$$\psi_4 = \int_{\xi} \frac{\kappa \left[\frac{1}{1 + \exp(\zeta \, \mathrm{f(x,y)})} - 0.5 H(\phi) \right]}{\Psi} dxdy ------(17)$$

$$\Psi = 1 + p\left(\xi_1 / I^* \right) p\left(\frac{\xi_2}{I^*} \right) \left\| \nabla G_\sigma \right| * \mathrm{I}^* \right|^{m+1} -----(18)$$

The variability of λ which controls the effect of weighted stopping length term [9].

A time variable 't', for which the energy function can be applied by applying Euler–Lagrange equation to obtain the evolution equation, can be obtained from equations (16),(17) and (18). In practice, a regularized continuous function of $\delta(\cdot)$ [9] by

$$\delta_\varepsilon = \frac{1}{\pi} \cdot \frac{\varepsilon^2}{1 + \varepsilon^2} ------(19)$$

where ε is a constant value.

The propose evolution curve from a partial differential equation which is driving elements for a curve to obtain boundaries and its corresponding energy model function equation (18) approaches to its minimum value.Due to thediffusion term in the exposedscheme which is nolonger needed [4]. Thus, equation (18) canbe attract by solving partial derivative in spatial coordinator and the forward difference scheme of partial derivative in temporal [4].

IV. RADON TRANSFORM

The main idea is to deduce the space search with parameter in order of decreasing the complexity of algorithm in 1 D space transform of a digital element. The Radon transform uses an angular profile utilization to achieve by radon [10]. The Radon transform of an image is consider as a total amount of the transforms of each individual pels of an image [8],[10]. A complete image should be categories in to four portion as separate sub digital elements describe in the figure 1.

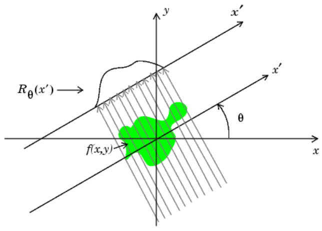

Figure: 1 Projection of Transformation of Radon.

The sub pixels of each pels contribute proportionally split with respect to the two nearest bins and also the projection location with bin as center in according with the distance metric. If the projection of a sub pixel with reference to the center point of bin to hit at each pels.

The Radon Transform is expressed as follows:

$$R_\gamma(r) = \iint_\xi f(x,y)\delta(x\cos\gamma + y\sin\gamma - r)dxdy ------(20)$$

Where R_γ is the Radon Transform of function f(x,y) at angle γ and δ is the Dirac function. So, when $\gamma = 0$ and $\gamma = \pi/2$.

V. EXPERIMENTAL RESULTS

In Experimental demonstration of a mammogram images contain abulkamount of mass with indefinite and multipart outlet portion wasexploited for evaluation purpose as shown in figures[2-4].

The method adapted for the evaluation of smooth front of mass by using thenon linear approach and stopping force function with weighted probability. The evaluation also calculated from initial level set function as shown in figures.

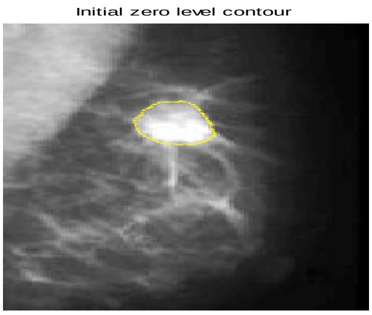

Figure:2,

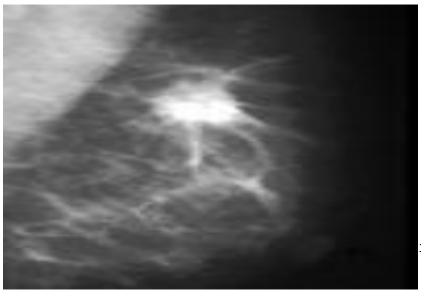

Figure:3,

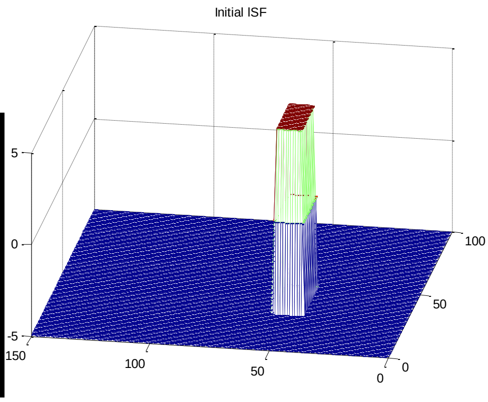

Figure:4,

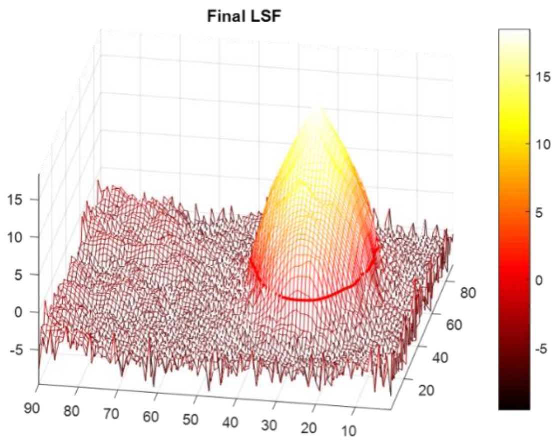

Figure : 5

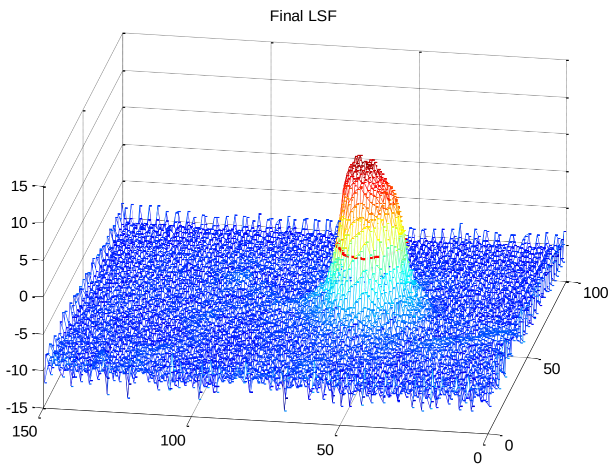

Figure :6

Figure 2: The initial Level Set Function
Figure 3: Input mammogram image
Figure 4: Contour on mammogram using nonlinear LSM Approach
Figure 5: Final Gaussian curve for final Level set function
Figure 6: Radon Transform for Final Level Set Function

VI. CONCLUSION AND DISCUSSION

This article construct novel approach of nonlinear with stopping force function based on probability weightedtoresolves problems which counter in early section. Anon-linear approach using LSF avoid the boundary leakages and probability weighting stopped function even in the presences of external noise. To extract the interest of region of a mammogram from an image and also its radon transform with level set function.Finally combustion of Radon transform for nonlinear approach of segmentation with Bayesian rulegives better results.

REFERENCES

1. L. Chen, C. L. P. Chen, and M. Lu, "A multiple-kernel fuzzy C-means algorithm for image segmentation," *IEEE Trans. Syst., Man, Cybern. B, Cybern.*, vol. 41, no. 5, pp. 1263–1274, Oct. 2011.
2. S. Osher and R. Fedkiw, "*Level Set Methods and Dynamics ImplicitSurfaces"*, New York, NY, USA: Springer-Verlag, 2003, chs. 3, 4.
3. R. Tsai and S. Osher, "Level set methods and their applications in image science," *Commun. Math. Sci.*, vol. 1, no. 4, pp. 1–20, Nov. 2003.
4. C. Li, C. Xu, C. Gui, and M. D. Fox, "Level set evolution without re-initialization: A new variational formulation," in *Proc. IEEE Conf. Comput. Vis. Pattern Recog.*, 2005, pp. 430–436.
5. T. F. Chan and L. A. Vese, "Active contours without edges," *IEEE Trans.Image Process.*, vol. 10, no. 2, pp. 266–277, Feb. 2001.
6. Y. Chen, D. Tseng, "Medical image segmentation based on Bayesian level set method," in *Proc. Med. Imag. Info*., 2007, pp. 25-34.
7. B.Wang,X.Fao,D.Tao and X.Li,"ANon linear adaptive Level set for Image Segmentation",*IEEETrans.onCybernetics*,Vol 44, No.3,March 2014.
8. R.Nirmala Devi, Tara Saikumar," Application of Radon Transform for Image Segmentation on Level set Method Using HKFCM Algorithm" Emerging ICT for Bridging the Future – Volume 1, Advances in Intelligent Systems and Computing 337, DOI: 10.1007/978-3-319-13728-5_29.
9. Bin Wang,XinboGao, Dacheng Tao, and Xuelong Li, " A Non Linear Adaptive Level Set for Image Segmentation", IEEE Transaction on Cybernetics, 2014.
10. Okman, O. Erman, and Gozde B. Akar. "A circle detection approach based on Radon Transform", 2013 IEEE International Conference on Acoustics Speech and Signal Processing, 2013.