

# LQR Based Optimal Control Techniques As Applied to Air Path of Diesel Engines

Shashidhar S Gokhale, Yathisha L, S Patil Kulkarni

**Abstract:** The selection of best optimal control technique for air path of diesel engines is a challenging task in the present scenario. Control inputs of air dynamics such as Exhaust Gas Recirculation (EGR), Variable Geometry Turbine (VGT) & Fuelling have different properties with respect to their different applications. Hence, in this paper different optimal LQR control techniques are proposed for all three control inputs of air dynamics in diesel engine. The proposed controllers have been implemented using MATLAB/SIMULINK® platform and the results are compared with the individual, coordinated & switching control inputs.

**Index Terms:** LQR, Optimal Control, Switched Linear Systems, EGR & VGT.

## I. INTRODUCTION

Air path is used in the diesel engines because it provides fresh air with necessary oxygen into the cylinders. To achieve this, a compressor, charge air cooler, intake and exhaust valves, Variable Geometry Turbocharger (VGT), Exhaust Gas Recirculation (EGR) valve, EGR cooler, Back Pressure Valve (BPV) and intake throttle can be used. Fig.1 shows the basic layout of an EGR engine (Chris Criens et al. 2014).

Exhaust Gas Recirculation (EGR) is a well known strategy to control NO<sub>x</sub> emissions in diesel engines. The EGR reduces NO<sub>x</sub> by reducing the oxygen concentration in the combustion chamber, as well as through temperature reduction. Variable Geometry Turbocharger (VGT) is designed such that the effective aspect ratio of the turbo to be varied as and when conditions change. In today's highly complex automotive system, selecting the better control input, controlling of overshoots, etc., for air path of diesel engines is very challenging. This has been a challenging research for the automotive control system community from last few decades. A brief literature survey of latest works in this area of research as below is motivation for the proposed work.

(Peter Ortner and Luigi del et al. 2007), describes the model based advanced control for the air path of diesel engines. The optimization problem is considered with input constraints and solved using model predictive algorithms. In (Stephan Zentner & Erika et al. 2014), the authors designed the control strategy to handle cross couplings of the system and the results are compared with a conventional controller of equal tuning.

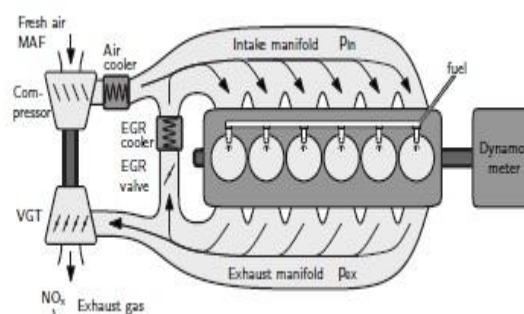


Fig 1: Layout of EGR Engine

For comparison, a single stage turbocharged diesel engine equipped with a HP EGR and VGT was used. (Mohamed Guermouche and Sofiane Ahmed Ali et al. 2014), developed a higher order sliding mode control technique for the internal combustion engine air path and the simulation results of air path engine model shows good results even under actuator faults conditions and in presence of parametric uncertainties. In (Peter Langthaler & Luigi del Re et al. 2014) the authors provide comparison of different robust predictive control strategies as applied to a Diesel engine airpath and the results conclude that the Robust Model Predictive Control (RMPC) technique provides better strategy than the standard engine control strategies which are tuned by system engineers. (Xiukun Wei and Luigi del Re et al. 2006), the authors proposed a pole placement method for Linear Parameter Varying (LPV) for the dynamics of the air path system and the simulation results show that the controller can achieve a performance which is satisfactory.

(M. Sassano & T. E. Passenbrunner et al. 2012), considered the problem of regulating fresh mass-air-flow and the absolute pressure in the intake-manifold in the air

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path of a turbocharged Diesel engine to set point references and the performances of the proposed control law have been validated by the simulation results. In (Tianpu Dong & Fujun Zhang et al. 2015), the authors proposed a novel approach for the control of diesel engine EGR system. The results are compared with the PID controller and it reveals that the proposed control for EGR engine system meet the well control requirements in steady and transient conditions.

In summary, a single optimized control input (EGR,VGT & Fuelling) will not be suitable at all over entire dynamic range of applications of today's complex automotive systems, particularly, in dynamics of air path system.

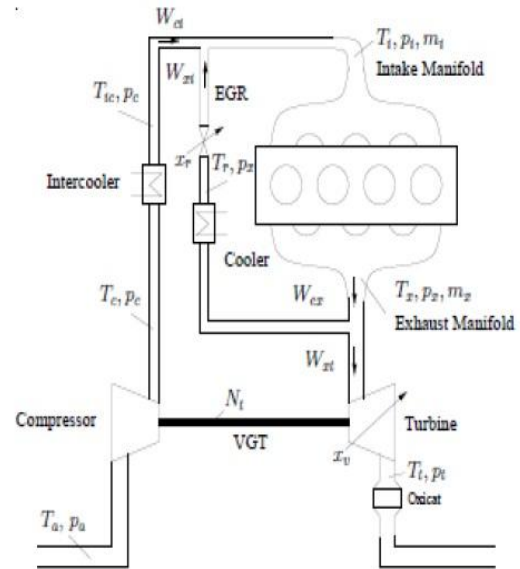
In the present work, Optimal Linear Quadratic Regulator (LQR) feedback control techniques are applied for EGR (B\_1), VGT (B\_2) & Fuelling (B\_3) control inputs in various capacities such as individually, coordinated & switching between individual control inputs. The proposed optimal control techniques are simulated using MATLAB/SIMULINK @ platform. Finally, the results are compared with respect to optimization (performance index  $J = \int_0^\infty y^2 dt$ ) peak overshoots & settling time to draw the conclusion to apply best optimal LQR control techniques in future.

The organization of remainder of the paper is as follows. Section II describes Linear Time Invariant (LTI) model investigation, plant properties of air path of diesel engines. Optimal control theory and the switched linear control theory are discussed in Sections III and IV respectively. Simulation results and discussions are presented in Section V and Section VI. Section VII concludes the paper.

## II. DYNAMIC MODEL: THE AIR PATH OF DIESEL ENGINES

The third order nonlinear mean value model parametrized for low and medium speed load points, covers the New European Drive Cycle (NEDC), was proposed by (Jung M et al. 2003) for robust control purposes. The System's basic structure is as shown in Fig. 2.

Parameter	Name
$\tau$	time constant of turbocharger
$\eta_m$	mechanical efficiency of turbocharger
$V_i$	Intake Manifold Volume
$V_x$	volume of the Exhaust Manifold
$\eta_c$	compressor efficiency
$T_a$	ambient temperature
$C_p$	Specific heat at constant pressure
$C_v$	Specific heat at constant volume
$\mu$	Specific heat ratio
$p_a$	ambient pressure
$T_x$	temperature of exhaust gas
$R$	gas constant
$n_v$	volumetric efficiency of engine
$T_i$	Intake Manifold gas temperature
$V_d$	total engine displacement volume
$p_{ref}$	reference pressure
$T_{ref}$	reference temperature
$\eta_t$	turbine efficiency
$n$	number of cylinders



**Fig 2:** Structure of Turbocharged Diesel Engine

$$\dot{p}_i = \frac{RT_i}{V_i} \left( \frac{n_c}{C_p T_a} \frac{p_c}{p_a^\mu} - 1 + \frac{A_{egr}(x_{egr} p_x)}{\sqrt{RT_x}} \sqrt{\frac{2p_i}{p_x} \left( 1 - \frac{p_i}{p_x} \right)} - n_v \frac{p_i N V_d}{120 T_i R} \right)$$

$$\dot{p}_x = \frac{RT_x}{V_x} \left( \frac{n_v p_i N V_d}{120 T_i R} + \frac{A_{egr}(x_{egr} p_x)}{\sqrt{RT_x}} \sqrt{2 \frac{p_i}{p_x} \left( 1 - \frac{p_i}{p_x} \right)} \right)$$

$$(-(ax_{vgt} + b) \left( c \left( \frac{p_x}{p_a} - 1 \right) + d \right) \frac{p_x}{p_{ref}} \sqrt{T_{ref} T_x} \sqrt{2 \frac{p_a}{p_x} \left( 1 - \frac{p_x}{p_a} \right)} + w_f)$$

$$\dot{p}_c = \frac{1}{\tau} (-p_c + \eta_m (ax_{vgt} + b) \left( c \left( \frac{p_x}{p_a} - 1 \right) + d \right) \frac{p_x}{p_{ref}} \sqrt{T_{ref} T_x} \sqrt{2 \frac{p_a}{p_x} \left( 1 - \frac{p_x}{p_a} \right)})$$

$$\left(\frac{p_x}{p_{ref}}\sqrt{\frac{T_{ref}}{T_x}}\sqrt{2\frac{p_a}{p_x}\left(1-\frac{p_a}{p_x}\right)c_pT_x\eta_t\left(1-\left(\frac{p_a}{p_x}\right)^\mu\right)}\right)$$

Table 1: Parameters of Nonlinear model

After linearization, the Linear Time Invariant (LTI) model can be written in state space as:

$$\begin{aligned}\Delta\dot{x} &= A.\Delta x + B.\Delta u \\ \Delta y &= C.\Delta x + D.\Delta u\end{aligned}$$

where,  $\Delta x = x - x_0$ ,  $\Delta u = u - u_0$ , and  $\Delta y = y - y_0$ ;  $A, B, C, D$  are the coefficient-matrices of the state space model. The Numerical values of  $A$  and  $B$  matrices used in the experiment are as follows:

$$A = \begin{bmatrix} -5.2643 & 4.7316 & 28.5021 \\ 50.7697 & -156.9827 & 0 \\ 0 & 0.4287 & -9.0909 \end{bmatrix}$$

$$B = \begin{bmatrix} 1.6111 \times 10^9 & 0 & 0 \\ -1.5720 \times 10^{10} & 8.3514 \times 10^4 & 1.46083 \times 10^8 \\ 0 & -141.6484 & 0 \end{bmatrix}$$

### III. OPTIMAL CONTROL THEORY

Optimal control theory is defined as control law searching for the given optimization problem which is in the quadratic form to obtain some optimization solution for that particular system. The advantage gained by using optimal control technique when compared to conventional pole placement technique is that the optimal control technique provides a coherent method of evaluating the closed loop control gain matrix. The optimized feedback controllers for this research are obtained from the LQR technique. A brief explanation of LQR is as follows (Yathisha L and S Patil Kulkarni et al. 2013; Yathisha L and S Patil Kulkarni et al. 2015; Yathisha L and S Patil Kulkarni et al. 2017):

#### A. Linear Quadratic Regulator: Individual & Coordinated Control Inputs

The minimization of performance index  $J$  can be achieved by optimal LQR state feedback control and also that guarantees the stability of the system.

Linear time invariant system

$$\begin{aligned}\dot{x}(t) &= A.x(t) + B.u(t) \\ y(t) &= C.x(t)\end{aligned}$$

The negative feedback system is given by

$$\dot{x}(t) = (A - BK).x(t)$$

Where  $K$  is the feedback controller gain. The performance

index  $J$  is given by,

$$J(x, u, Q, R) = \int_0^\infty (x^T.Qx + u^T.Ru).dt, \quad Q \geq 0, R \geq 0$$

The aim of the LQR problem is to design a control law  $u = -Kx$  by minimizing the objective function  $J$  with the solution given by,

$$K = -R^{-1}.B^T.P$$

Thus the control law is

$$u(t) = -K.x(t) = -R^{-1}.B^T.P \quad (2)$$

In which  $P$  must satisfy the reduced Riccati equation,

$$P.A + A^T.P - P.B.R^{-1}.B^T.P + Q = 0 \quad (3)$$

By using the MATLAB command `lqr`, the algebraic Riccati equation is computed.

$$[K, P, E] = \text{lqr}(A, B, Q, R)$$

#### B. Linear Quadratic Regulator: Switching Control

Switched systems are the combination of two or more control inputs to combine the properties of all the control inputs and it is guided by a switching law.

#### Advantages of Switching Control

- Switching between two feedback control structure is to select the best control structure for the particular application.
- If any of the component failure in one of the control structure, the switching supervisor will take care of the same and alternate control will be in place.

A switched linear system model for this research is as follows:

$$\dot{x} = A_\sigma x(t)$$

The switching signal  $\sigma(t)$  indicates

$$\begin{aligned}\dot{x}(t) &= A_\alpha x(t) = \text{if}, \quad \sigma = \alpha \\ &= A_\beta x(t) = \text{if}, \quad \sigma = \beta \\ &= A_\gamma x(t) = \text{if}, \quad \sigma = \gamma\end{aligned}$$

Where,

$$A_\alpha = A - B_1 K_1$$

$$A_\beta = A - B_2 K_2$$

$$A_\gamma = A - B_3 K_3$$

Here,  $B_1$  = EGR,  $B_2$  = VGT &  $B_3$  = Fuelling control inputs and the feedback controllers  $K_1$ ,  $K_2$  &  $K_3$  are derived from the optimal LQR theory by tuning of the weighting matrices.



### Switching Control Algorithm

The existing switching algorithm by (Lalitha S Devarakond et al. 2006; Yathisha L et al. 2018) is as follows (Ex: For  $B_1$  &  $B_2$  control inputs):

- Initialize the two closed loop systems  $A_\alpha$  &  $A_\beta$ .

- Determine  $T_0$  by solving the Lyapunov

Equation:

$$A_\alpha^T T_0 + T_0 A_\alpha = -C^T \cdot C$$

- Using,  $A_2$  the switching matrix is defined as:

$$S = -(A_\beta^T T_0 + T_0 A_\beta + C^T C)$$

- Now, the switching rule is that,

$$\sigma = \beta \quad \text{if } \langle x, Sx \rangle > 0 \\ \sigma = \alpha \quad \text{otherwise}$$

### IV. EXPERIMENTAL SETUP

The proposed novel optimal LQR control techniques for all the control inputs are investigated by considering the following cases:

**Case I.(i):** Optimal LQR feedback controller  $K_1$  is designed for the control input  $B_1$ .

**Case I.(ii):** Optimal LQR feedback controller  $K_2$  is designed for the control input  $B_2$ .

**Case I.(iii):** Optimal LQR feedback controller  $K_a$  is designed for the coordinated control input  $B_a = [B_1 \ B_2]$ .

**Case I.(iv):** Switching between the control inputs  $B_1$  and  $B_2$  is considered for this case.  $K_1$  &  $K_2$  corresponding to their  $B_1$  &  $B_2$  are updated and defined as shown in Table 3.

Table 3: Updated controller gains for switching

$B$	$K_1$	$K_2$
$[B_1 \ B_2]$	$k'_1 = \begin{bmatrix} K_1 \\ 0 \end{bmatrix}$	$k'_2 = \begin{bmatrix} 0 \\ K_2 \end{bmatrix}$

**Case II.(i):** Optimal LQR feedback controller  $K_2$  is designed for the control input  $B_2$ .

**Case II.(ii):** Optimal LQR feedback controller  $K_3$  is designed for the control input  $B_3$ .

**Case II.(iii):** Optimal LQR feedback controller  $K_b$  is designed for the coordinated control input  $B_b = [B_2 \ B_3]$ .

**Case II.(iv):** Switching Between the control inputs  $B_2$  and  $B_3$  is considered for this case.  $K_2$  &  $K_3$

corresponding to their  $B_2$  &  $B_3$  are updated and defined as shown in Table 4.

Table 4: Updated controller gains for switching

$B$	$K_2$	$K_3$
$[B_2 \ B_3]$	$k'_2 = \begin{bmatrix} K_2 \\ 0 \end{bmatrix}$	$k'_3 = \begin{bmatrix} 0 \\ K_3 \end{bmatrix}$

**Case III.(i):** Optimal LQR feedback controller  $K_3$  is designed for the control input  $B_3$ .

**Case III.(ii):** Optimal LQR feedback controller  $K_1$  is designed for the control input  $B_1$ .

**Case III.(iii):** Optimal LQR feedback controller  $K_c$  is designed for the coordinated control input  $B_c = [B_3 \ B_1]$ .

**Case III.(iv):** Switching Between the control inputs  $B_3$  and  $B_1$  is considered for this case.  $K_3$  &  $K_1$  corresponding to their  $B_3$  &  $B_1$  are updated and defined as shown in Table 5.

Table 5: Updated controller gains for switching

$B$	$K_2$	$K_3$
$[B_3 \ B_1]$	$k'_3 = \begin{bmatrix} K_3 \\ 0 \end{bmatrix}$	$k'_1 = \begin{bmatrix} 0 \\ K_1 \end{bmatrix}$

**Case IV.(i):** Optimal LQR feedback controller  $K_a$  is designed for the coordinated control input  $B_a = [B_1 \ B_2]$ .

**Case IV.(ii):** Optimal LQR feedback controller  $K_b$  is designed for the coordinated control input  $B_b = [B_2 \ B_3]$ .

**Case IV.(iii):** Switching Between the coordinated control inputs  $B_a = [B_1 \ B_2]$  &  $B_b = [B_2 \ B_3]$  is considered for this case.  $K_a$  &  $K_b$  corresponding to their  $B_a$  &  $B_b$  are updated and defined as shown in Table 6.

Table 6: Updated controller gains for switching

$B = [B_1 \ B_2 \ B_3]$	$K_a / K_b$
$B_a = [B_1 \ B_2]$	$k'_a = \begin{bmatrix} K_{11} \\ K_{21} \\ 0 \end{bmatrix}$
$B_b = [B_2 \ B_3]$	$k'_b = \begin{bmatrix} 0 \\ K_{11} \\ K_{21} \end{bmatrix}$

**Case V.(i):** Optimal LQR feedback controller  $K_b$  is designed for the coordinated control input  $B_b = [B_2 \ B_3]$ .

**Case V.(ii):** Optimal LQR feedback controller  $K_c$  is designed for the coordinated control input



$$B_c = [B_3 \ B_1].$$

**Case V.(iii):** Switching Between the coordinated control inputs  $B_b = [B_2 \ B_3]$  &  $B_c = [B_3 \ B_1]$  is considered for this case.  $K_b$  &  $K_c$  corresponding to their  $B_b$  &  $B_c$  are updated and defined as shown in Table 7.

Table 7: Updated controller gains for switching

$B = [B_1 \ B_2 \ B_3]$	$K_a / K_b$
$B_b = [B_2 \ B_3]$	$k'_b = \begin{bmatrix} 0 \\ K_{11} \\ K_{21} \end{bmatrix}$
$B_c = [B_3 \ B_1]$	$k'_c = \begin{bmatrix} K_{11} \\ 0 \\ K_{21} \end{bmatrix}$

**Case VI.(i):** Optimal LQR feedback controller  $K_c$  is designed for the coordinated control input  $B_c = [B_3 \ B_1]$ .

**Case VI.(ii):** Optimal LQR feedback controller  $K_a$  is designed for the coordinated control input  $B_a = [B_1 \ B_2]$ .

**Case VI.(iii):** Switching Between the coordinated control inputs  $B_c = [B_3 \ B_1]$  &  $B_a = [B_1 \ B_2]$  is considered for this case.  $K_c$  &  $K_a$  corresponding to their  $B_c$  &  $B_a$  are updated and defined as shown in Table VII.

Table 8: Updated controller gains for switching

$B = [B_1 \ B_2 \ B_3]$	$K_c / K_a$
$B_c = [B_3 \ B_1]$	$k'_c = \begin{bmatrix} K_{11} \\ 0 \\ K_{21} \end{bmatrix}$
$B_a = [B_1 \ B_2]$	$k'_a = \begin{bmatrix} K_{11} \\ K_{21} \\ 0 \end{bmatrix}$

## V. SIMULATION RESULTS

To do the comparison of all the proposed optimal LQR control techniques, simulations are carried out for all the state space variables, Intake manifold pressure ( $p_i$ ), Exhaust manifold pressure ( $p_x$ ) & Turbine power ( $p_c$ ) deviations. The numerical values of the optimized LQR feedback controller gains  $K_1, K_2, K_3, K_a, K_b$  &  $K_c$  are as follows:

$$K_1 = [0.2883 \ -0.9757 \ 0.0527 \ ]$$

$$K_2 = [0.4080 \ 0.9994 \ 0.7540 \ ]$$

$$K_3 = [0.4245 \ 1.0000 \ 0.8033 \ ]$$

$$K_a = \begin{bmatrix} -3.2296 \times 10^{-9} & -7.3747 \times 10^{-7} & -0.9998 \\ 4.1696 \times 10^{-7} & -8.9701 \times 10^{-9} & -0.0024 \end{bmatrix}$$

$$K_b = \begin{bmatrix} 8.9321 \times 10^{-11} & -9.2463 \times 10^{-7} & -0.0247 \\ 3.4753 \times 10^{-7} & 7.5465 \times 10^{-5} & 0.9981 \end{bmatrix}$$

$$K_c = \begin{bmatrix} 1.1474 \times 10^{-9} & 6.8645 \times 10^{-8} & 0.0093 \\ -3.2189 \times 10^{-9} & -7.3742 \times 10^{-6} & -0.9998 \end{bmatrix}$$

The dynamic response of the state variables  $p_i, p_x$  &  $p_c$  for all the cases are shown in Figures 3-13.

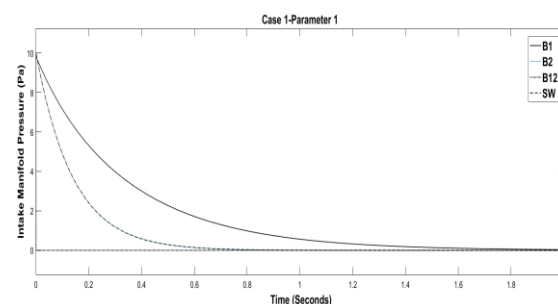


Fig 3:  $p_i$  Case I response

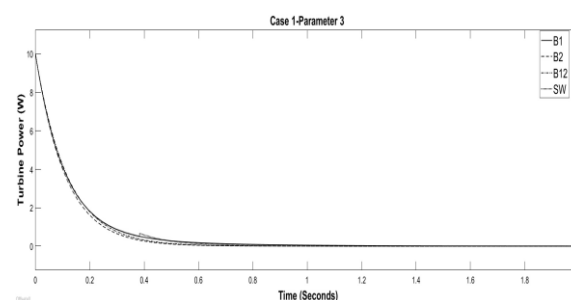


Fig 4:  $p_c$  Case I response

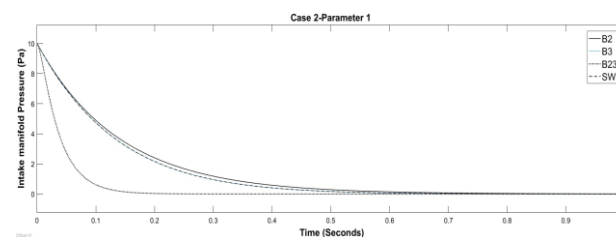


Fig 5:  $p_i$  Case II response

# LQR Based Optimal Control Techniques As Applied To Air Path of Diesel Engines

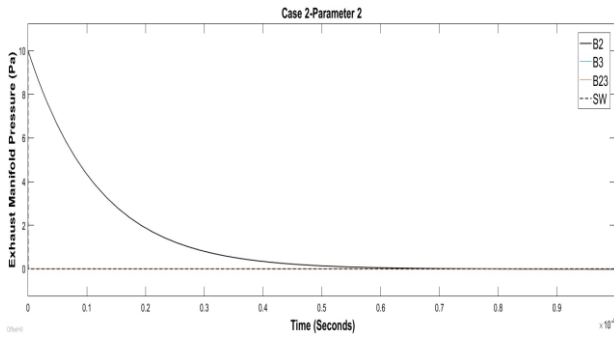


Fig 6:  $p_x$  Case II response

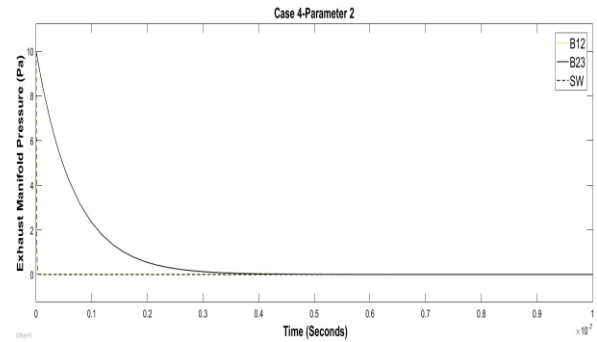


Figure 10:  $p_x$  Case IV response

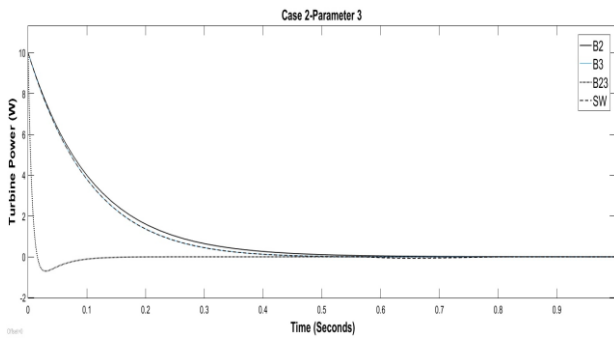


Figure 7:  $p_c$  Case II response

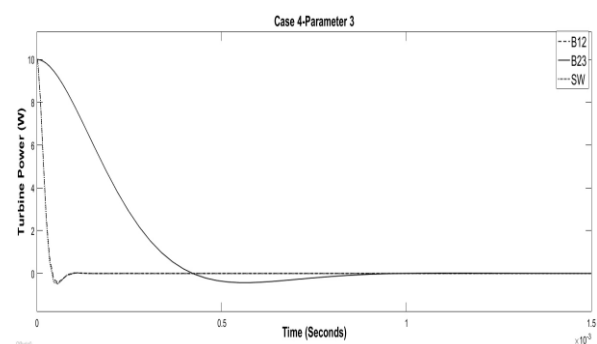


Figure 11:  $p_c$  Case IV response

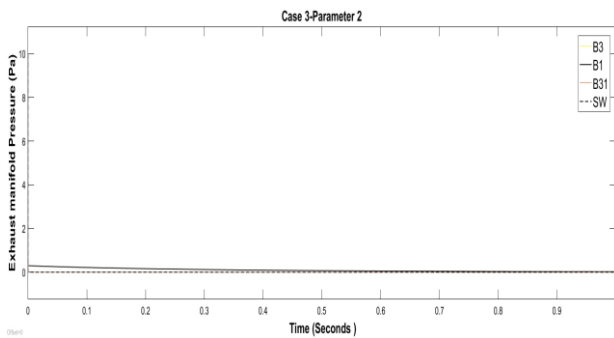


Figure 8:  $p_x$  Case III response

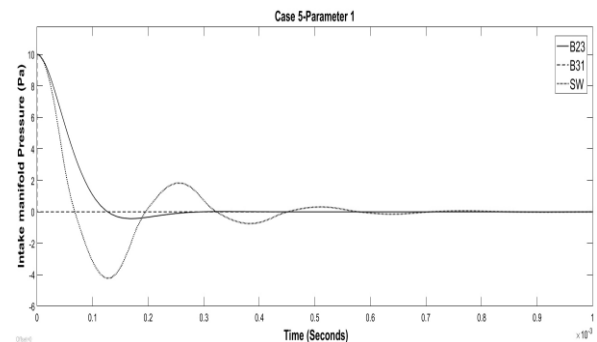


Figure 12:  $p_i$  Case V response

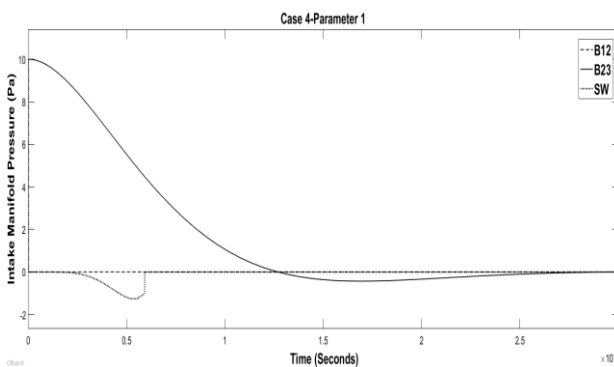


Figure 9:  $p_i$  Case IV response

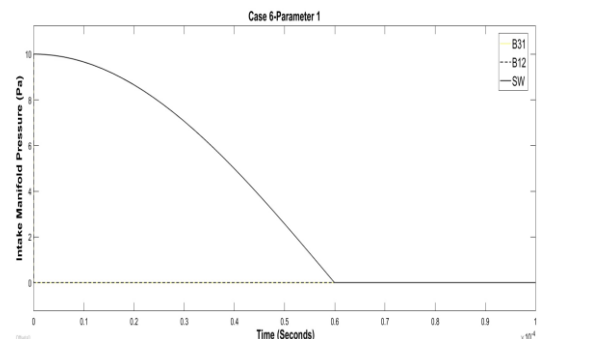


Figure 13:  $p_i$  Case VI response

**Table 9:** performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case I

State Variables	$B_1 K_1$	$B_2 K_2$	$B_a K_a$	Switch $B_1 K_1 / B_2 K_2$
$p_i$	15.92	6.984	0.005746	6.984
$p_x$	$1.382 \times 10^{-5}$	0.00059	$6.071 \times 10^{-7}$	0.0005
$p_c$	5.697	5.451	5.791	5.697

**Table 10:** Performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case II

State Variables	$B_2 K_2$	$B_3 K_3$	$B_b K_b$	Switch $B_2 K_2 / B_3 K_3$
$p_i$	6.984	6.635	2.181	6.635
$p_x$	0.0005	$3.517 \times 10^{-7}$	$3.517 \times 10^{-7}$	$3.517 \times 10^{-7}$
$p_c$	5.451	5.158	0.2981	5.158

**Table 11:** performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case III

State Variables	$B_3 K_3$	$B_1 K_1$	$B_c K_c$	Switch $B_3 K_3 / B_1 K_1$
$p_i$	6.635	15.92	$3.276 \times 10^{-6}$	6.635
$p_x$	$3.517 \times 10^{-7}$	$1.382 \times 10^{-5}$	$3.695 \times 10^{-9}$	$3.517 \times 10^{-7}$
$p_c$	5.158	5.697	5.492	5.158

**Table 12:** performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case IV

State Variables	$B_a K_a$	$B_b K_b$	Switch $B_a K_a / B_b K_b$
$p_i$	0.005746	2.181	$2.41 \times 10^{-5}$
$p_x$	$6.071 \times 10^{-7}$	$3.517 \times 10^{-7}$	$3.281 \times 10^{-9}$
$p_c$	5.791	0.2981	0.001284

**Table 13:** performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case V

State Variables	$B_b K_b$	$B_c K_c$	Switch $B_b K_b / B_c K_c$
$p_i$	2.181	$3.276 \times 10^{-6}$	0.0004306
$p_c$	0.2981	5.492	15.06

**Table 14:** performance index ( $J = \int_0^\infty y^2 dt$ ) Comparison for Case VI

State Variables	$B_c K_c$	$B_a K_a$	Switch $B_c K_c / B_a K_a$
$p_i$	$3.276 \times 10^{-6}$	0.0057	0.002992
$p_c$	5.492	5.791	173.5

## VI. DISCUSSION

Figures 3-13 and Tables IX -XIV shows the dynamic response plots of  $p_i$ ,  $p_x$  &  $p_c$  and comparison of

performance index  $J$  for all the cases defined in the experimental set up. The discussions of the experimental results are as follows:

**Case I:** The simulation results of individual controllers  $B_1 K_1$ ,  $B_2 K_2$ , coordinated control inputs ( $B_a K_a$ ) and switch between individual controllers ( $B_1 K_1 / B_2 K_2$ ) reveals that for the state space variables  $p_i$  &  $p_x$  the coordinated control design ( $B_a K_a$ ) provides better performance and for the state variable  $p_c$  the individual control input  $B_2 K_2$  gives good results with respect to the optimization.

**Case II:** For all the three state variables ( $p_i$ ,  $p_x$  &  $p_c$ ) the coordinated control inputs of VGT & Fuelling ( $B_b K_b$ ) has better response compared to other proposed control techniques.

**Case III:** The simulation results for this case shows that for the deviations in intake and exhaust manifold pressures ( $p_i$  &  $p_x$ ) the coordinated control design ( $B_c K_c$ ) provides better results and for the turbine power deviation ( $p_c$ ) the switching between two individual control inputs ( $B_3 K_3 / B_1 K_1$ ) has lesser performance index( $J$ ) compared to other control input techniques.

**Case IV:** In this case, the experiment set-ups are conducted for the coordinated control inputs and the simulation results indicate that for all the three state variables ( $p_i$ ,  $p_x$  &  $p_c$ ), the switching control technique between two coordinated control inputs ( $B_a K_a / B_b K_b$ ) provide better output performance in comparison to without switching (Individual coordinated control inputs ( $B_a K_a$ ) & ( $B_b K_b$ )).

**Case V:** The simulation results in this case reveals that for the state variable  $p_i$  the coordinated control inputs  $B_c K_c$  and for  $p_c$  the coordinated control inputs  $B_b K_b$  provides better performance. The simulation result for the state variable  $p_x$  introduces error in plots.

**Case VI:** The coordinated control inputs  $B_a K_a$  provides good results compared to other control techniques for the state variables  $p_i$  &  $p_c$  and for the state variable  $p_x$  introduces error in plots.

## VII. CONCLUSION

The summary of the literature survey indicates that the control techniques proposed by different authors in most of the papers are briefed on stability of the system by applying faults for the existing air dynamics state space model at different times. In this paper the different optimal LQR control techniques are applied for the three control inputs EGR, VGT & Fuelling of air dynamics in existing state space model in various combinations by developing six cases of different experimental set ups.

All the proposed six cases are simulated using MATLAB/SIMULINK@ platform and the results are compared with respect to the optimization level of output performance ( $J = \int_0^\infty y^2 dt$ ). Since, the proposed control techniques combine more than one

controller, hence concentrating only on the minimization of output energy by neglecting the control energy. The output performance is very much essential for the air path of diesel engines.

Figures 3-13 and Tables IX -XIV, for different control technique simulation results conclude that case IV result of switching control techniques between the coordinated control inputs ( $B_a K_a / B_b K_b$ ) provides very good response and also the performance index ( $J$ ) is minimized in comparison with all other control techniques of different cases. In future, the proposed control technique can be applied for the system with disturbances or by applying different faults.

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