

A Refinement on E-Path Partial Redundancy Elimination

Rahibb, S Sarala

Abstract: *Partial redundancy elimination algorithm is a compiler optimization method that eliminates expressions that are redundant on some programming path but not necessarily all paths in a Data Flow Graph (DFG) of a program. The E-Path Partial Redundancy Elimination algorithm authored by DM Dhamdhere for Partial Redundancy Elimination (PRE) of common subexpression elimination does not give much importance to the elimination of edge splitting, even though the edge splitting is much more expensive than inserting an expression in an existing node of a DFG of a program. So in this paper we try to refine the E-Path PRE algorithm with a new equation for inserting expressions at nodes avoiding edge splitting as far as possible and hence the E-Path PRE algorithm becomes more compact and beautiful.*

Keywords: *Data Flow Graph, Partial Redundancy Elimination, Availability, Anticipability, E_path suffix.*

I. INTRODUCTION

The redundancy of an expression in a program can exist in the form of common subexpression, a loop-invariant expression, and it can be partial redundancy too, if it is found along some of the paths, but not necessarily along all paths. A Partially Redundant Elimination (PRE) algorithm is an optimization technique for transforming partial redundancy of an expression in a program into fully redundancy and eliminate the redundancy. A PRE algorithm is considered to be optimal if no other PRE algorithm gives a data flow graph which contains fewer computations (less insertions and more deletions) in any path in the data flow graph.

The Morel E and Renvoise C [1] first proposed a bi-directional algorithm for code optimization in compilers in 1979, by suppressing partial redundancies such as moving loop invariant computation out of a loop or deleting redundant computations. The algorithm is referred to as MRA. The MRA algorithm was updated by DM Dhamdhere and SM Joshi [2] by including strength reduction techniques. However, when there is a loop invariant expression that cannot be moved to a node out of the loop, the MRA fails, because it performs insertions strictly in nodes of a data flow graph, and it does not support the edge splitting at all. And the MRA lacks both computational and life time optimality also.

The Edge Placement Algorithm [3] by DM Dhamdhere, called EPA, performs insertions both in nodes and along edges in a DFG. In this algorithm an expression is hoisted as far up as possible to obtain computational optimality, and then it is subjected to sinking to get lifetime optimality without sacrificing computational optimality. However EPA does not provide lifetime optimality in some cases.

The research papers [4] and [5] developed for enhancing PRE algorithm to eliminate partial redundancies of expressions in a computer program.

The problem lies with the paper [4], hoisting-by-sinking, is that the conceptual complexity is so high that it is hard to understand and implement in a compiler. There are research papers [6], [7] and [10] that do not use hoisting-by-sinking method. However, the paper [6] suffers from the unnecessary edge splitting. But unlike the paper [11] says, the paper [10] does avoid the edge splitting by using a conditional statement in its algorithm.

The PRE algorithm used in the paper [7] is used in the text book [8] and in [9] though, the splitting of the edges before the analysis of the program results in unnecessary edge splitting.

DM Dhamdhere [11] proposed a unidirectional data flow analysis algorithm for partial redundancy elimination which is computationally and lifetime optimal. Though the edge splitting is more expensive than inserting an expression at an existing node [3],[11], the E-Path PRE algorithm does not give much care for eliminating them. In this paper we give an alteration to the insert equation at nodes of the E-Path PRE algorithm to remove the edge splitting of a DFG as much as possible and hence to make the algorithm more beautiful and attractive.

II. E-PATH_PRE ALGORITHM BY DM DHAMDHERE

DM Dhamdhere presented the E-Path algorithm [11]. The algorithm first identifies the insertion points at nodes and on edges and then identify the saves points, and finally the redundant occurrences of an expression for replacement. The Table 1 summarizes the data flow properties and equations of the algorithm. Let e be an expression in a node, i of a DFG. The local data flow property $anticip_loc_i$ represents a locally anticipated upwards exposed e in node, i , $compute_i$ represents a locally available downwards exposed e in node, i , and $trans_i$ reflects the absence of assignments to the operand(s) of e in node, i . Global properties of availability, anticipability and E-path suffix are used to collect global information. $insert_i$ and $insert_{i,j}$ identify e to be inserted in node, i , and on edge (i,j) respectively, and $save_i$ identifies the node b_i in which e should be saved.

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compute _i	:	e is nearby existing in b _i
anticip_loc _i	:	e is nearby anticipatable in b _i
trans _i	:	b _i does not include an assignment to any of the operands of e
avail_in _i /avail_out _i	:	e is existing at entry/exit of b _i
anticip_in _i /anticip_out _i	:	e is anticipatable at entry/exit of b _i
e_ps_in _i /e_ps_out _i	:	entry/exit of b _i is in an e-path suffix
redund _i	:	incidence of e in b _i is redundant
insert _i	:	insert temp _e ← e in node b _i
insert _{ij}	:	insert temp _e ← e on edge (b _i ,b _j)
save_in _i /save_out _i	:	e must be kept above the entry/exit of b _i
save _i	:	e should be kept in temp _e in node b _i

Table 1 : E-PATH Partial Redundancy Elimination

Data Flow Properties

Data Flow Equations

avail_in _i	:	$\prod_{p \in pred(i)} av_out_p$
avail_out _i	:	avail_in _i .trans _i + compute _i
anticip_in _i	:	anticip_out _i .trans _i + anticip_loc _i
anticip_out _i	:	$\prod_{s \in succ(i)} anticip_in_s$
e_ps_in _i	:	$\sum_{p \in pred(i)} (avail_out_p + e_ps_out_p) anticip_in_i \neg avail_in_i$
e_ps_out _i	:	e_ps_in _i . ¬anticip_loc _i
redund _i	:	(avail_in _i + e_ps_in _i).anticip_loc _i
insert _i	:	¬avail_out _i . ¬e_ps_out _i . $\prod_{s \in succ(i)} e_ps_in_s$
insert _{ij}	:	¬insert _i ¬avail_out _i . ¬e_ps_out _i . e_ps_in _j
save_out _i	:	$\sum_{s \in succ(i)} (e_ps_in_s + redund_s + save_in_s) . avail_out_i$
save_in _i	:	save_out _i . ¬compute _i
save _i	:	save_out _i .compute _i .¬(redund _i .trans _i)

III. A REFINEMENT

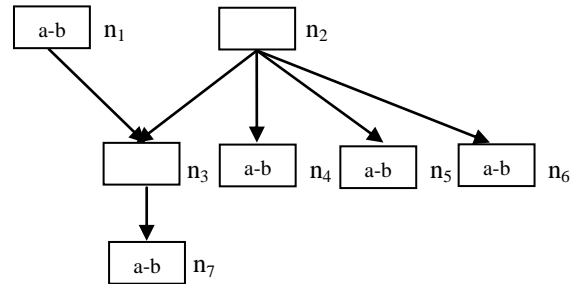
Consider the control flow graph of Fig.1(a) consisting of 7 nodes. Here the E_Path_PRE is n₁-n₃-n₇. So the E_PATH_PRE algorithm saves the expression a*b at n₁ in a temporary variable t and replaces it in the node n₇ with t. Since $\prod_{s \in succ(n_2)} E_PS_IN_s = \text{False}$ for the node n₂, insertion of the computation at node n₂ is not possible according to the E-Path PRE algorithm. But insertion on the edge (n₂,n₃) is possible since INSERT₂₃ is true as shown in the Fig.1(b). But if we apply the new equation shown in the Table 2, we get the Fig.1(c). According to the lemma III in the E_Path PRE algorithm an expression in a node can be eliminated if and only if that expression is available at beginning of that node in the optimized program. In Fig.1(c) the expression a-b is available at the entry of nodes n₄,n₅,n₆ and n₇, and hence the expression a-b from them are deleted. The application of the new INSERT equation has 2 advantages. One is that it eliminates the edge splitting as much as possible, and the second is it replaces isolated expressions from the nodes to some extent without sacrificing the computational and life time optimality of the E-Path PRE algorithm. The expression

a-b at nodes n₄, n₅, and n₆ in Fig.1(a) are the isolated expressions because the E-Path PRE algorithm cannot form E-paths for them. However, they are deleted by the new equation as shown in Fig.1(c).

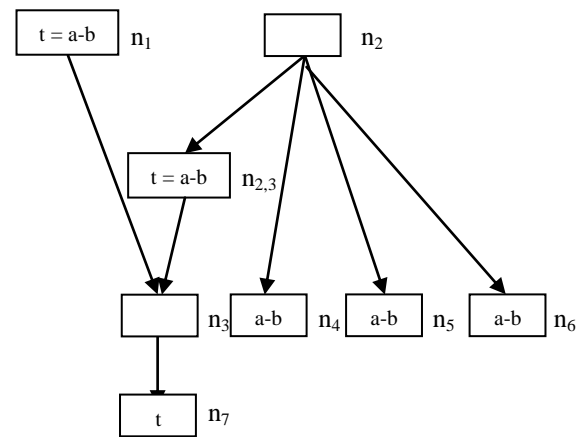
Table 2 : A Refinement on E_Path PRE Algorithm

$$INSERT_i = \neg AV_OUT_i . \neg EPS_OUT_i . \sum_{s \in succ(i)} EPS_IN_s . \prod_{s \in succ(i)} ANT_IN_s$$

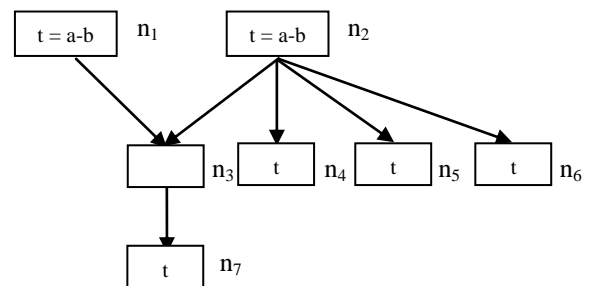
All other equations remain the same as in the PRE algorithm.



(a) before PRE



(b) after E_Path PRE



(c) after applying new equation

Fig.1. Partial Redundancy Elimination

IV. CONCLUSION

The E-Path PRE algorithm, by DM Dhamdhere did not take care of eliminating edge splitting much, even though the edge splitting is much more expensive than inserting a computation in an existing node. In this paper we added much care for avoiding edge splitting as far as possible to make the E-Path PRE algorithm more refined and compact. In this paper we updated the $INSERT_i$ equation to eliminate the edge splitting as much as possible. And the refined algorithm is also computationally and lifetime optimal.

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